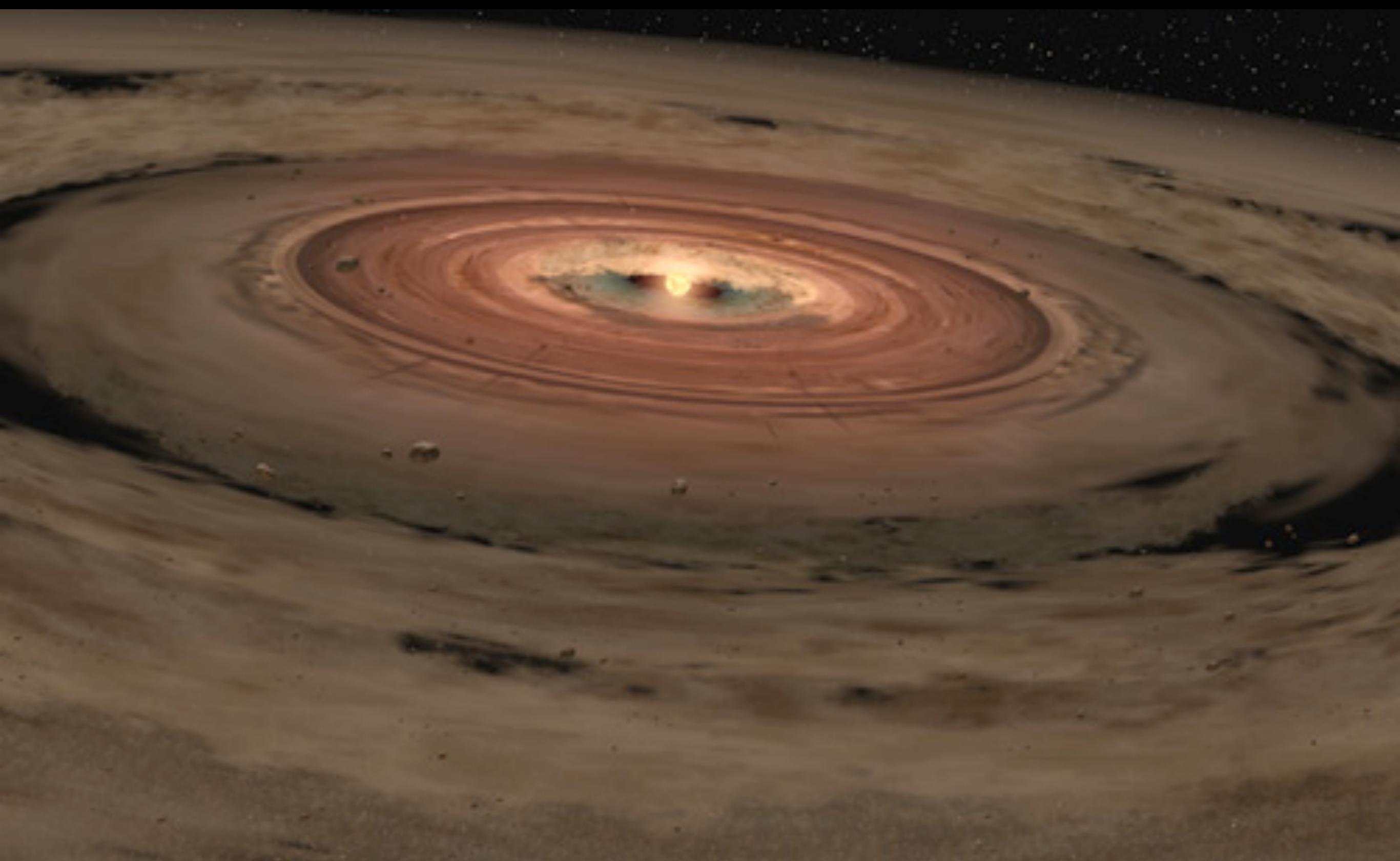


# Astrophysics of Planet Formation

## Lecture 5 - Planet migration



# Course Outline

- 5 Lectures, 2 hours each (with a break in the middle!).
  - 1) Observations of planetary systems
  - 2) Protoplanetary discs
  - 3) Dust dynamics & planetesimal formation
  - 4) Planet formation
  - 5) Planetary dynamics
- Notes for each lecture will be placed on the course home page in advance - you may find it useful to annotate these as we go.
- These slides will also be posted online.
- Textbooks: Armitage - *Astrophysics of planet formation* (CUP).  
*Protostars & Planets* series (V - 2007; VI - 2014)



# Resonant Torques

- Full perturbation analysis finds that the total torque is the sum of the torques at resonances.

- Co-rotation resonance:

$$\Omega(R) = \Omega_p$$

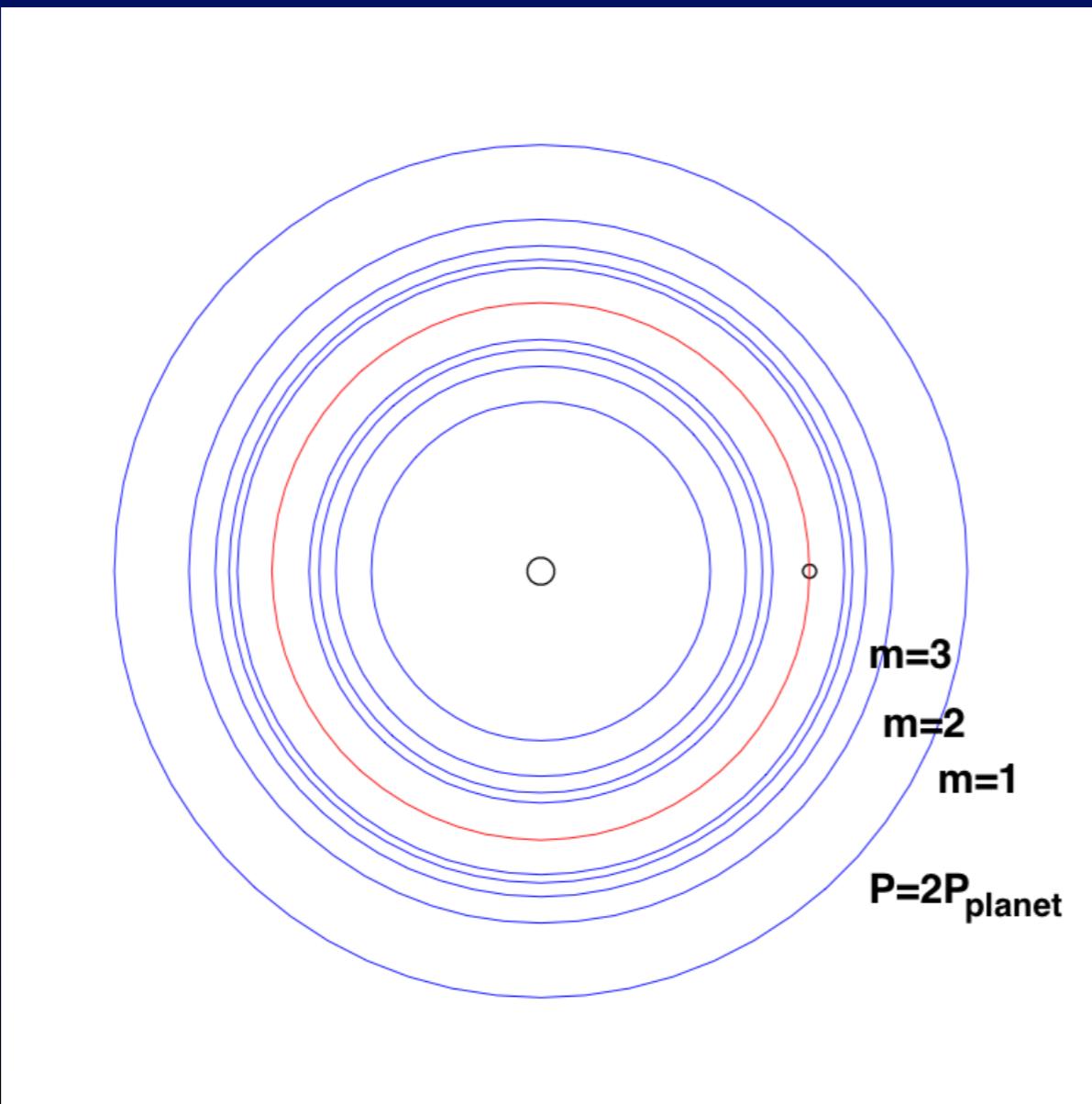
- Lindblad resonances:

$$m[\Omega(R) - \Omega_p] = \pm \kappa(R)$$

$$R_L = \left( 1 \pm \frac{1}{m} \right)^{2/3} a$$

# Resonant Torques

- Circular disc has one co-rotation resonance and a “comb” of Lindblad resonances:



$$R_L = \left( 1 \pm \frac{1}{m} \right)^{2/3} a$$

Figure from Armitage (2007)

# Resonant Torques

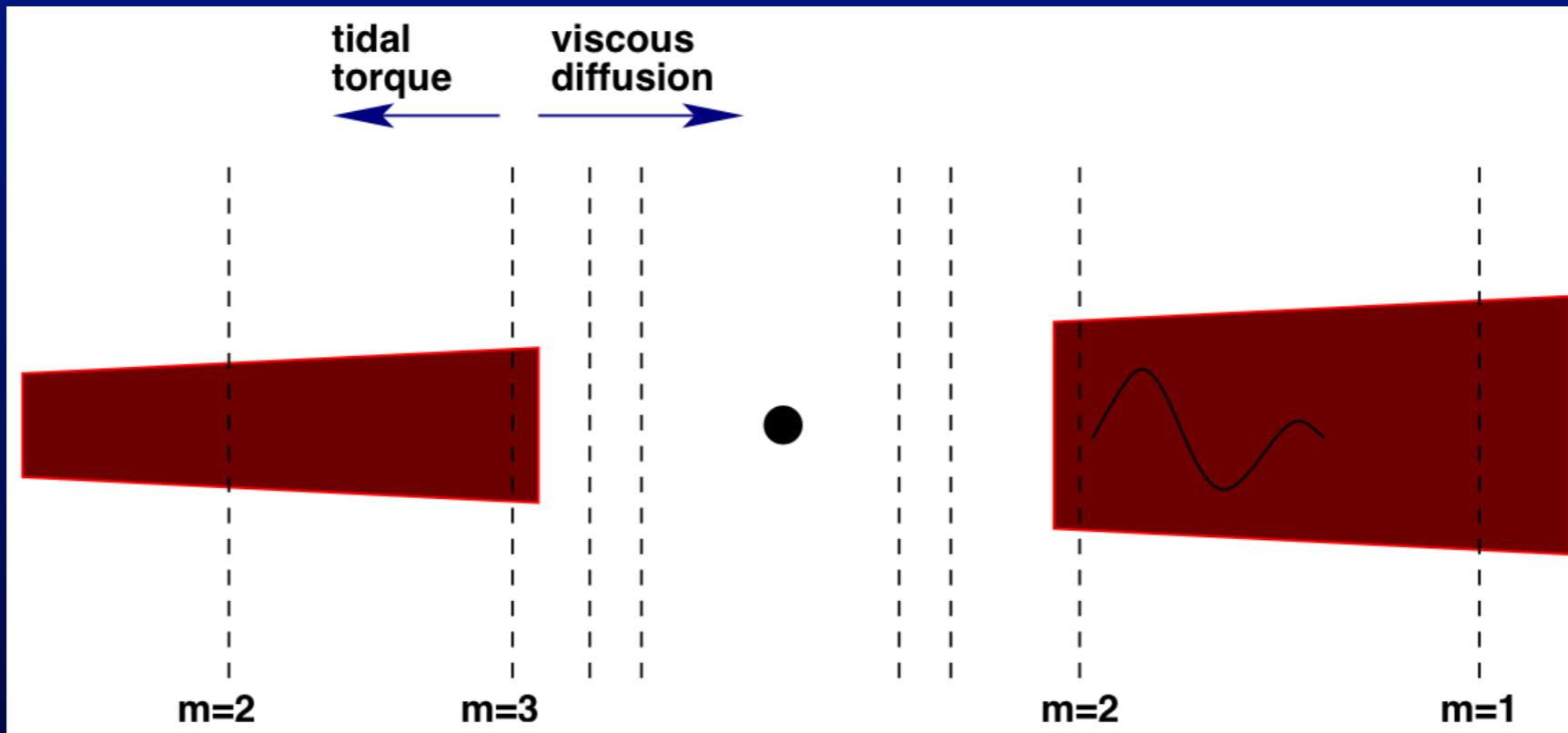


Figure from Armitage (2007)

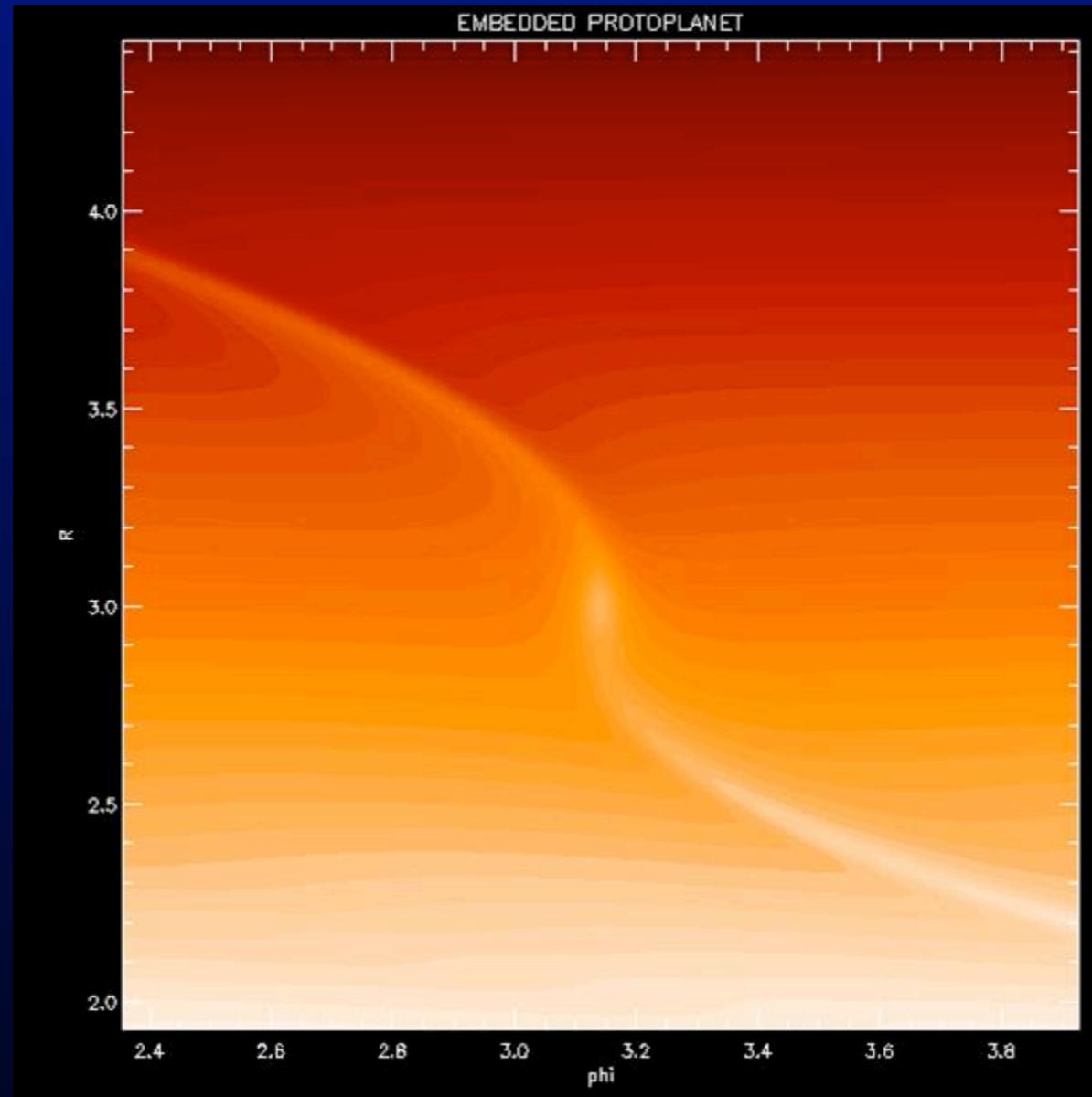
- Torques repel disc gas from region close to planet, but viscosity opposes this. A sufficiently massive planet can open a gap in the disc.
- For typical disc parameters, the gap-opening mass is a few times the mass of Saturn.

No gap = Type I migration

Gap = Type II migration

# Type I migration in real discs

Figures/movies from Nelson et al. (2003,2004)

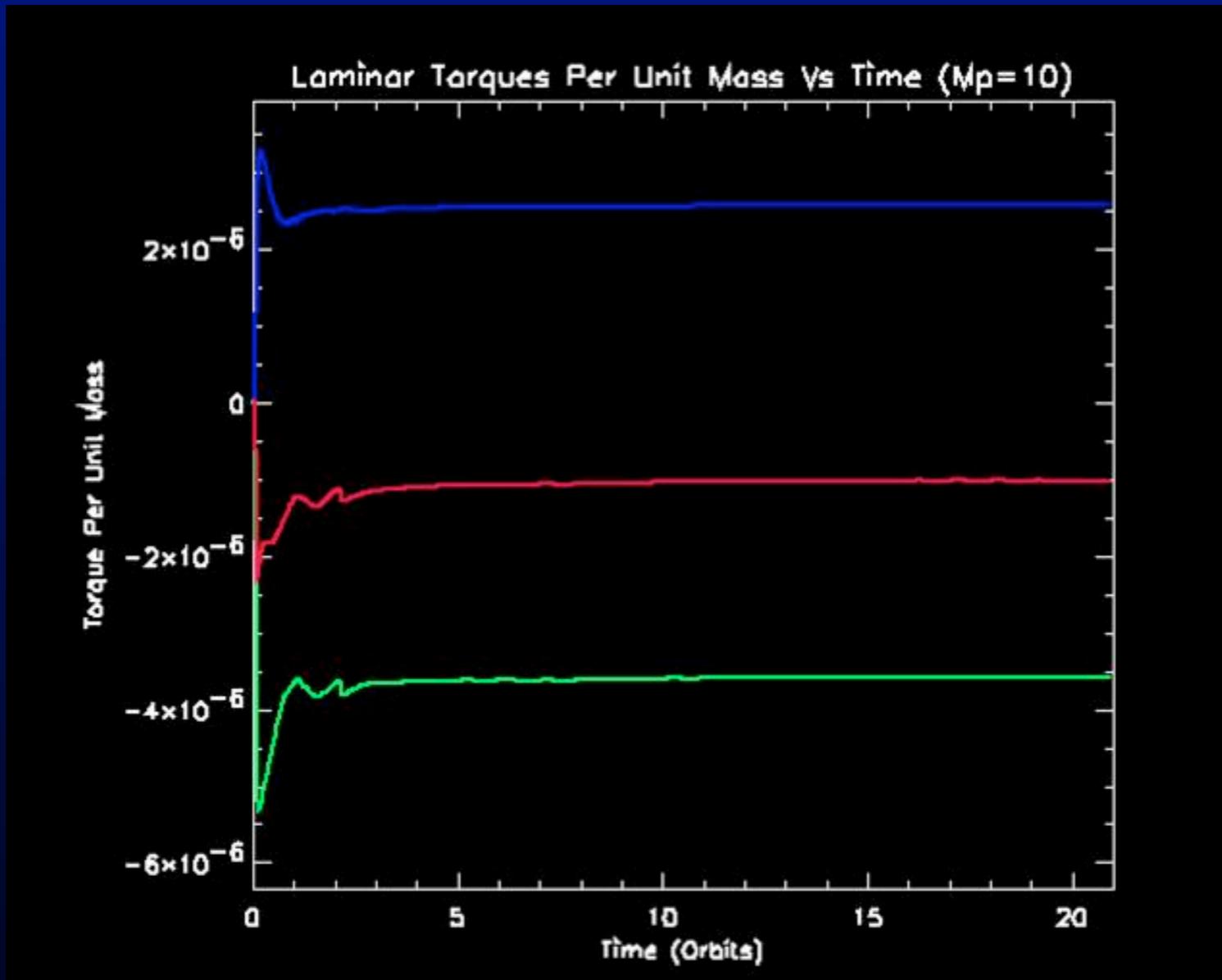


$10M_{\oplus}$  planet in laminar disc:

Spiral density waves launched from resonances. Well-defined, stable torques drive steady migration.

# Type I migration in real discs

Figures/movies from Nelson et al. (2003,2004)

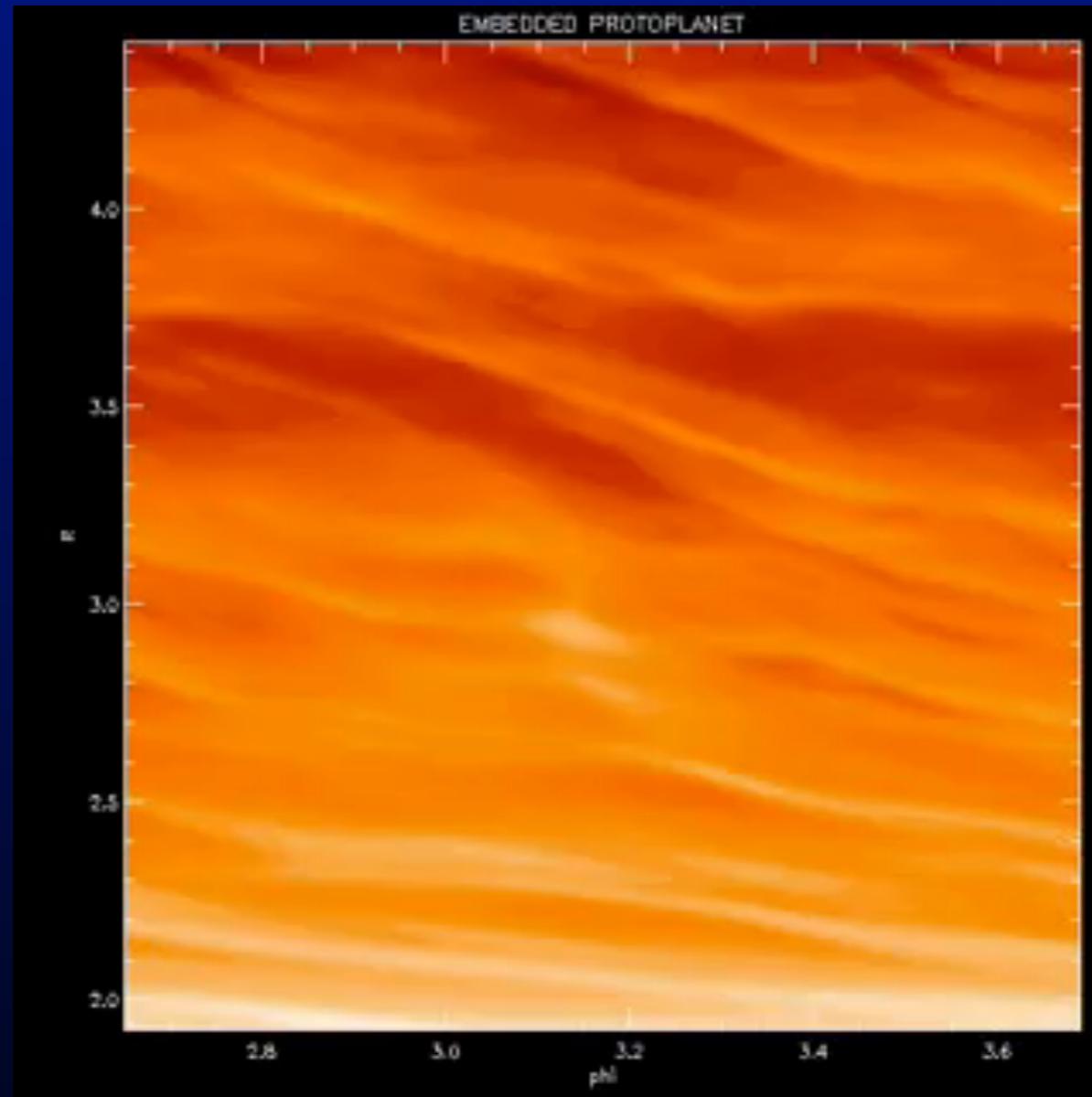


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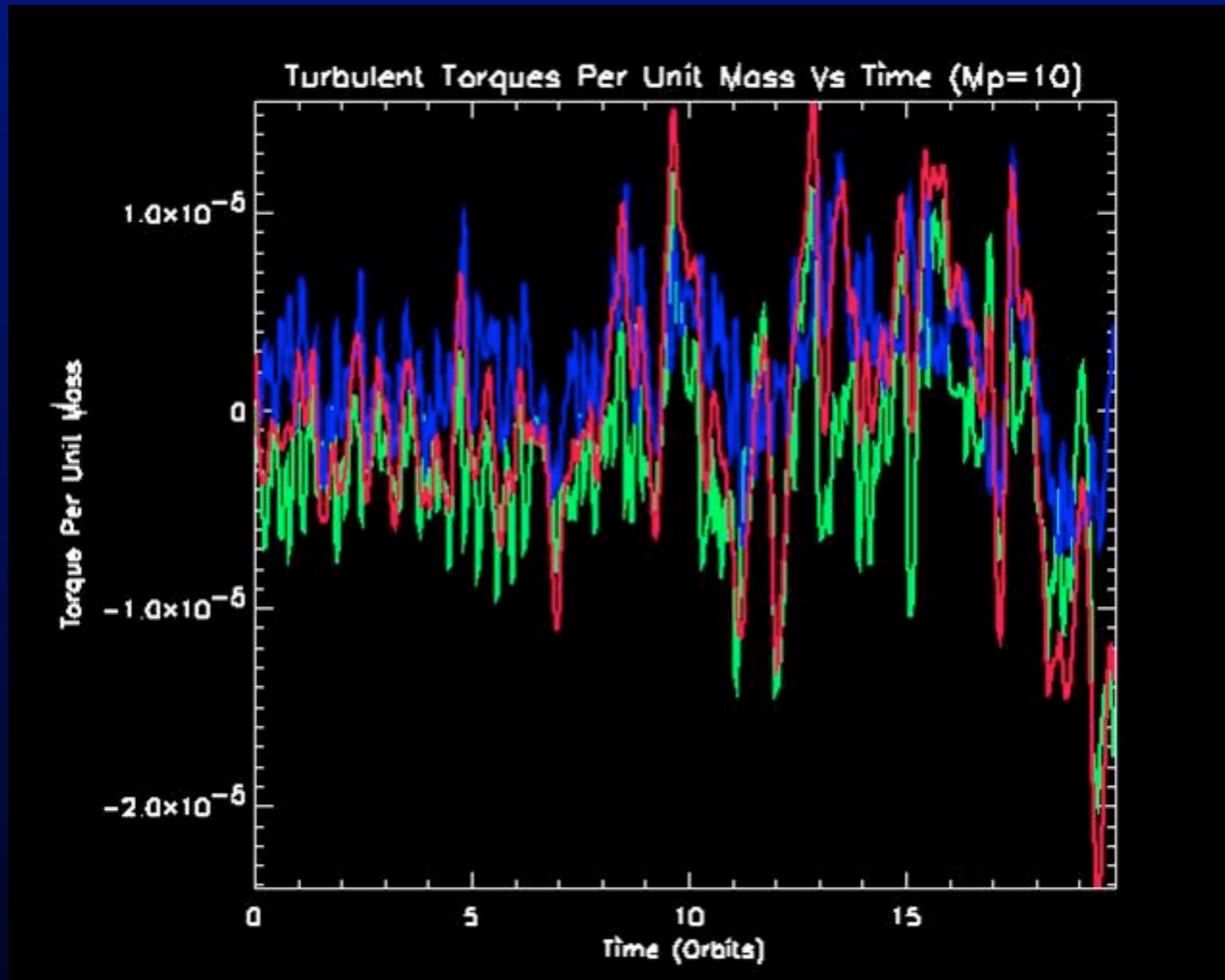


$10M_{\oplus}$  planet in MRI-turbulent disc:

Spiral density waves dwarfed by turbulent fluctuations.  
Torques are very variable, leading to stochastic migration.

# Type I migration in real discs

Figures/movies from Nelson et al. (2003,2004)

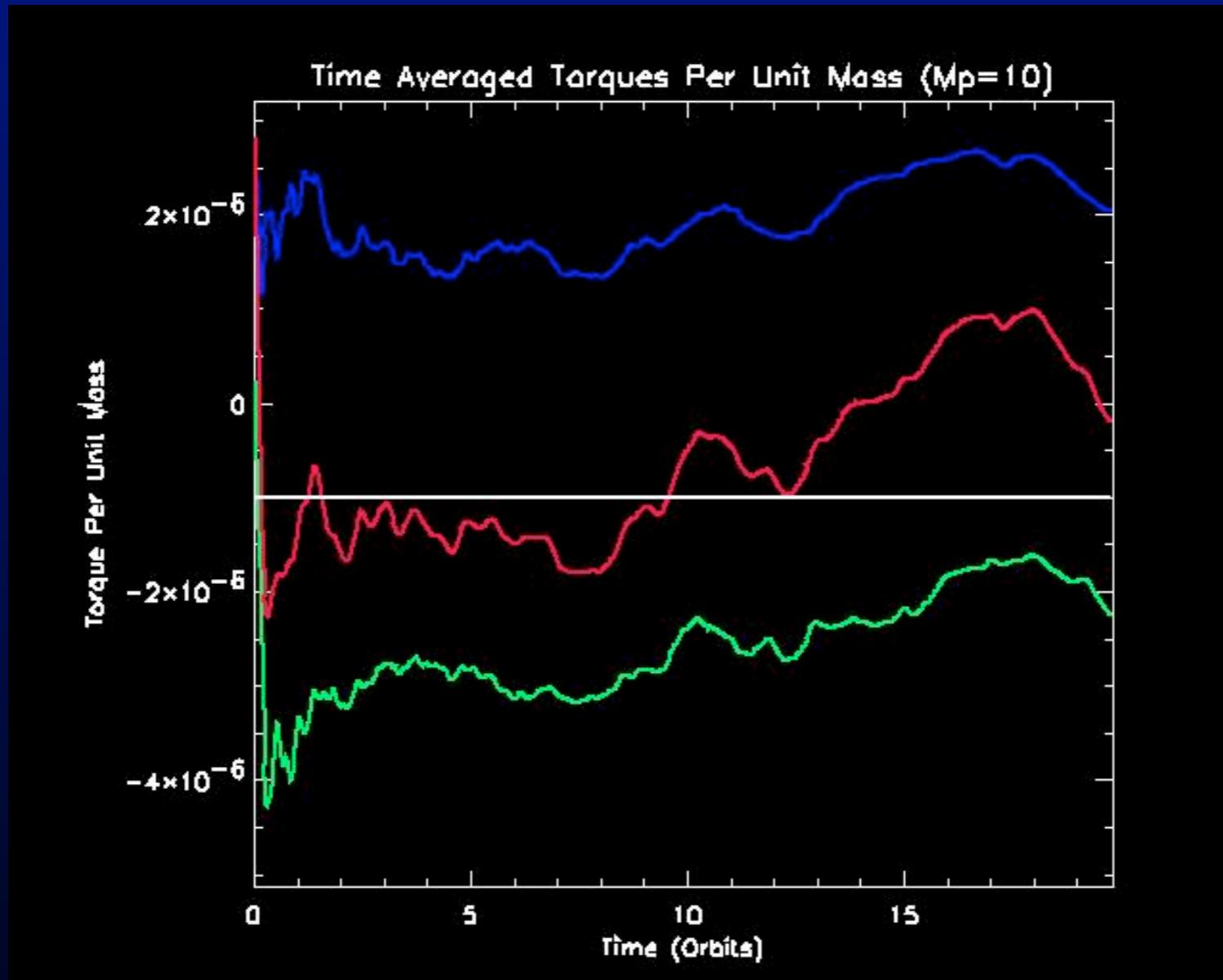


$10M_{\oplus}$  planet in MRI-turbulent disc:

Spiral density waves dwarfed by turbulent fluctuations.  
Torques are very variable, leading to stochastic migration.

# Type I migration in real discs

Figures/movies from Nelson et al. (2003,2004)

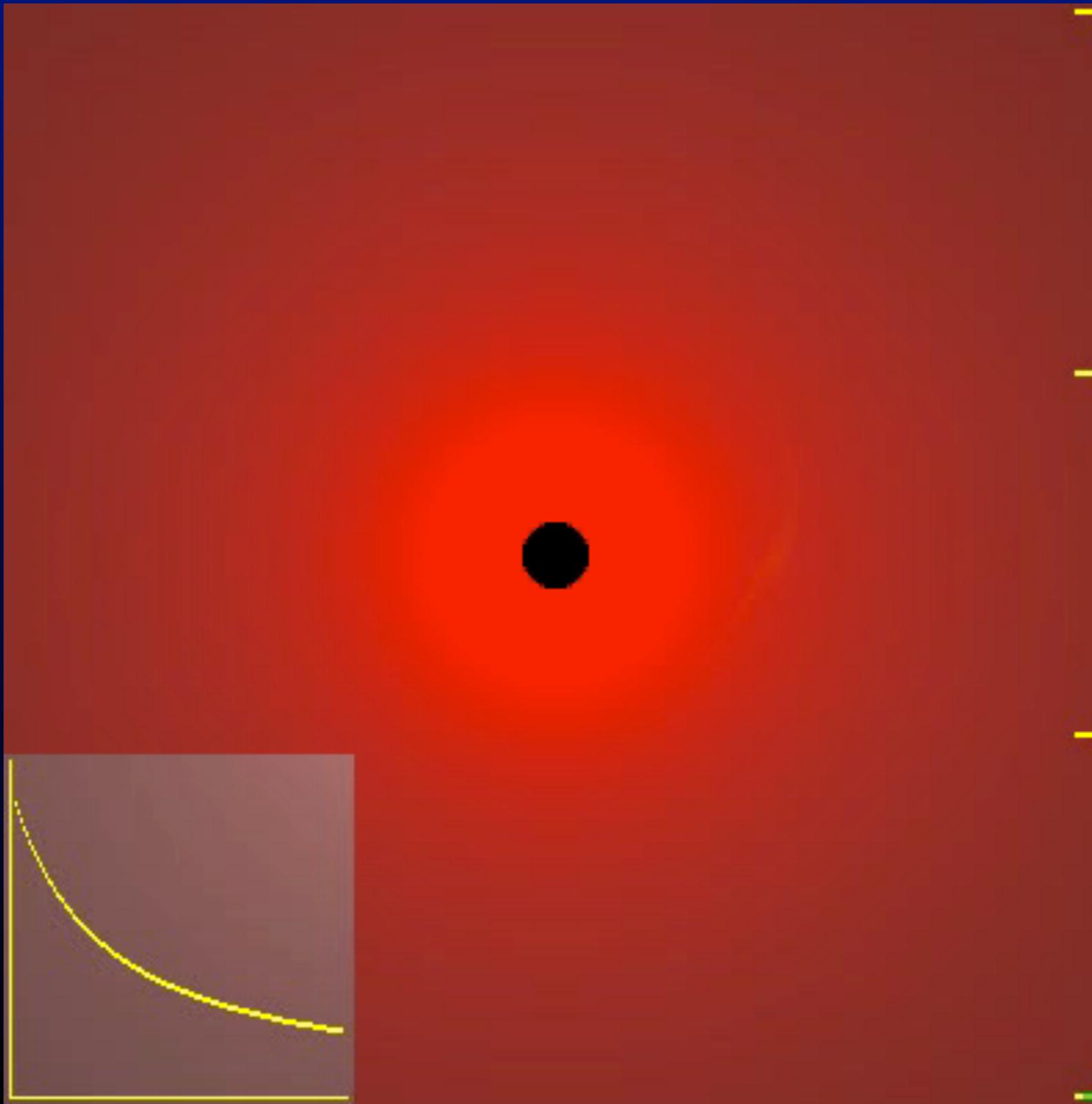


$10M_\oplus$  planet in MRI-turbulent disc:

Spiral density waves dwarfed by turbulent fluctuations.  
Torques are very variable, leading to stochastic migration.

# Type I/II migration

Animation from Armitage (2005)





# Resonant capture

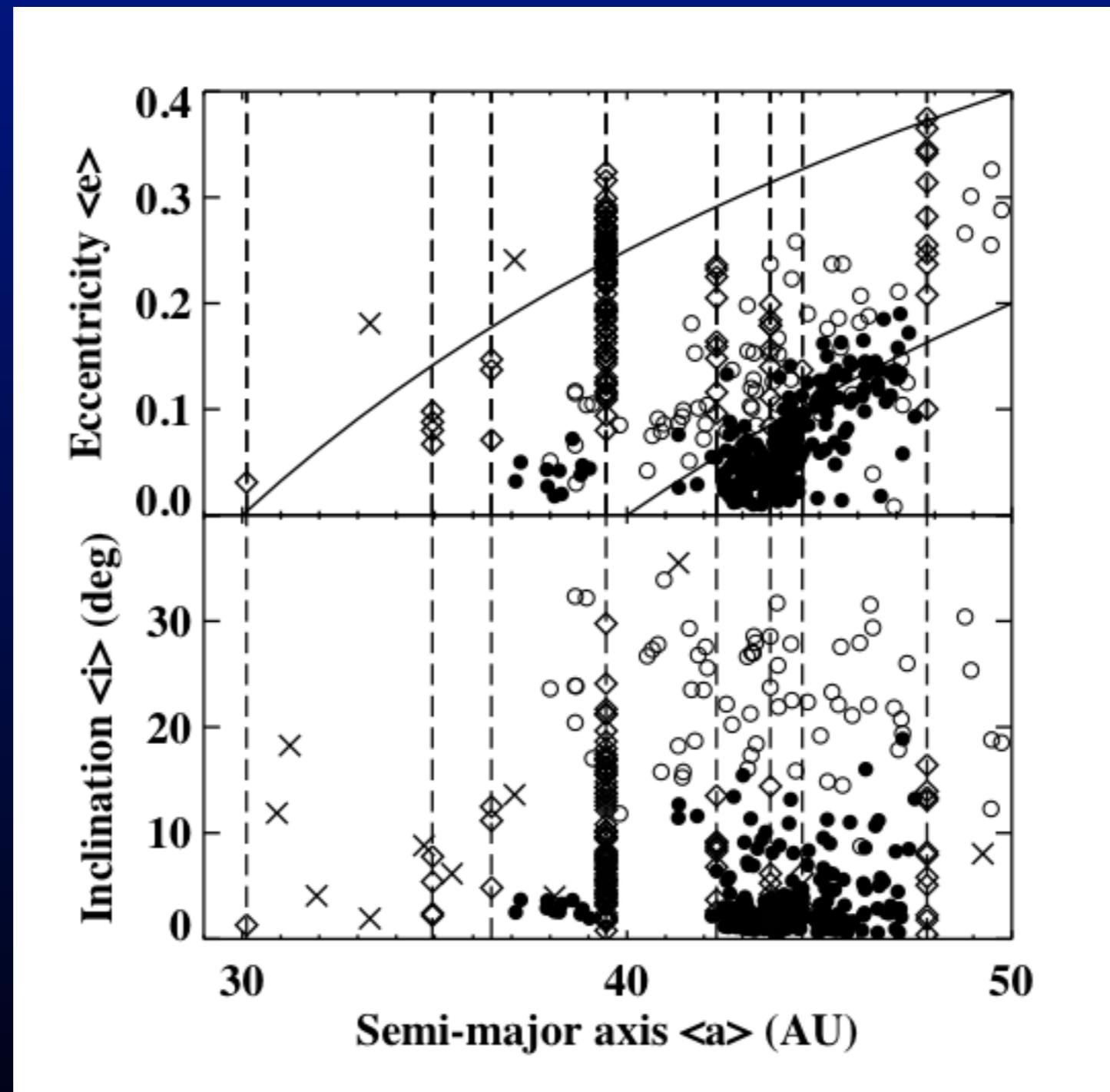
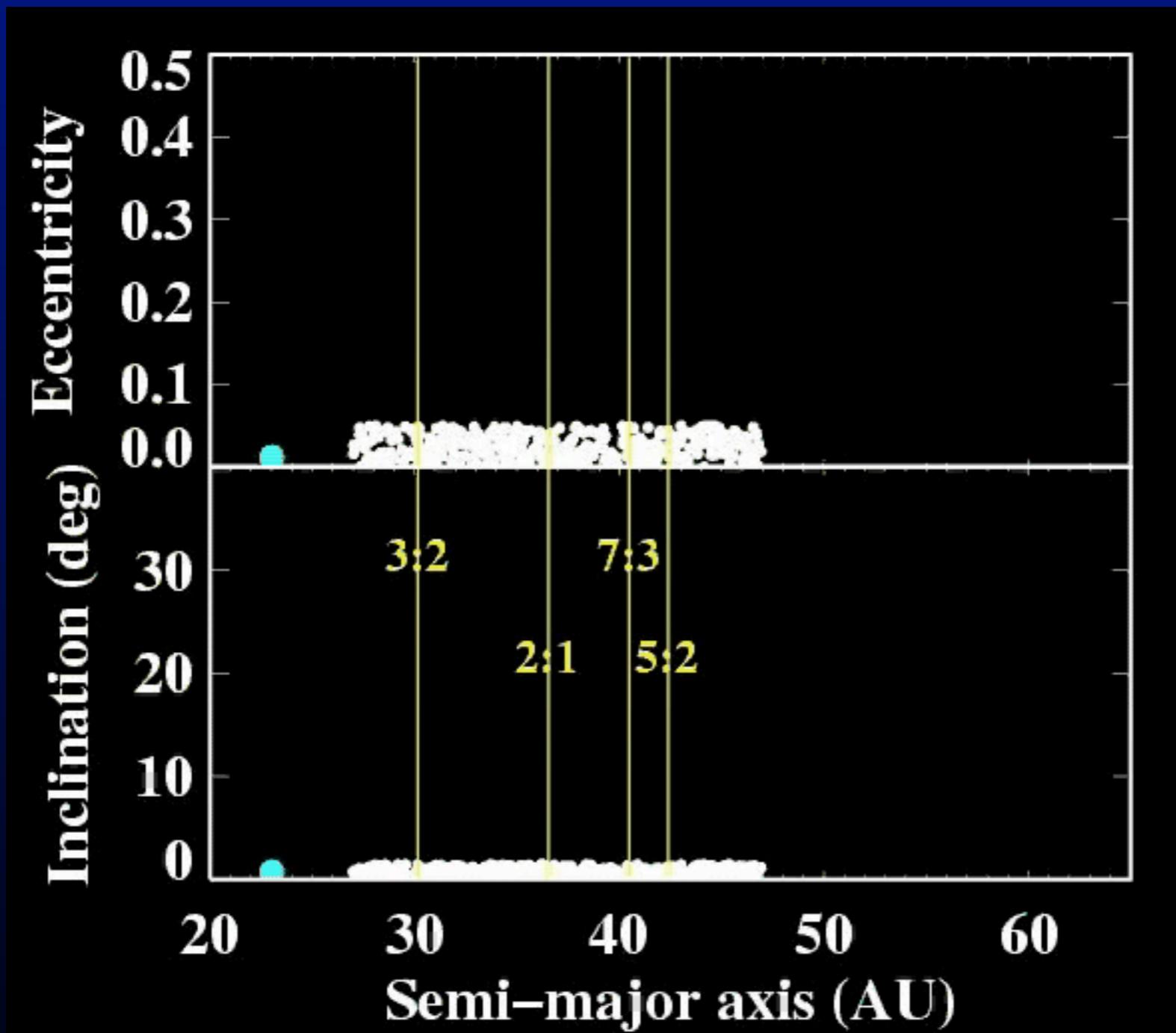


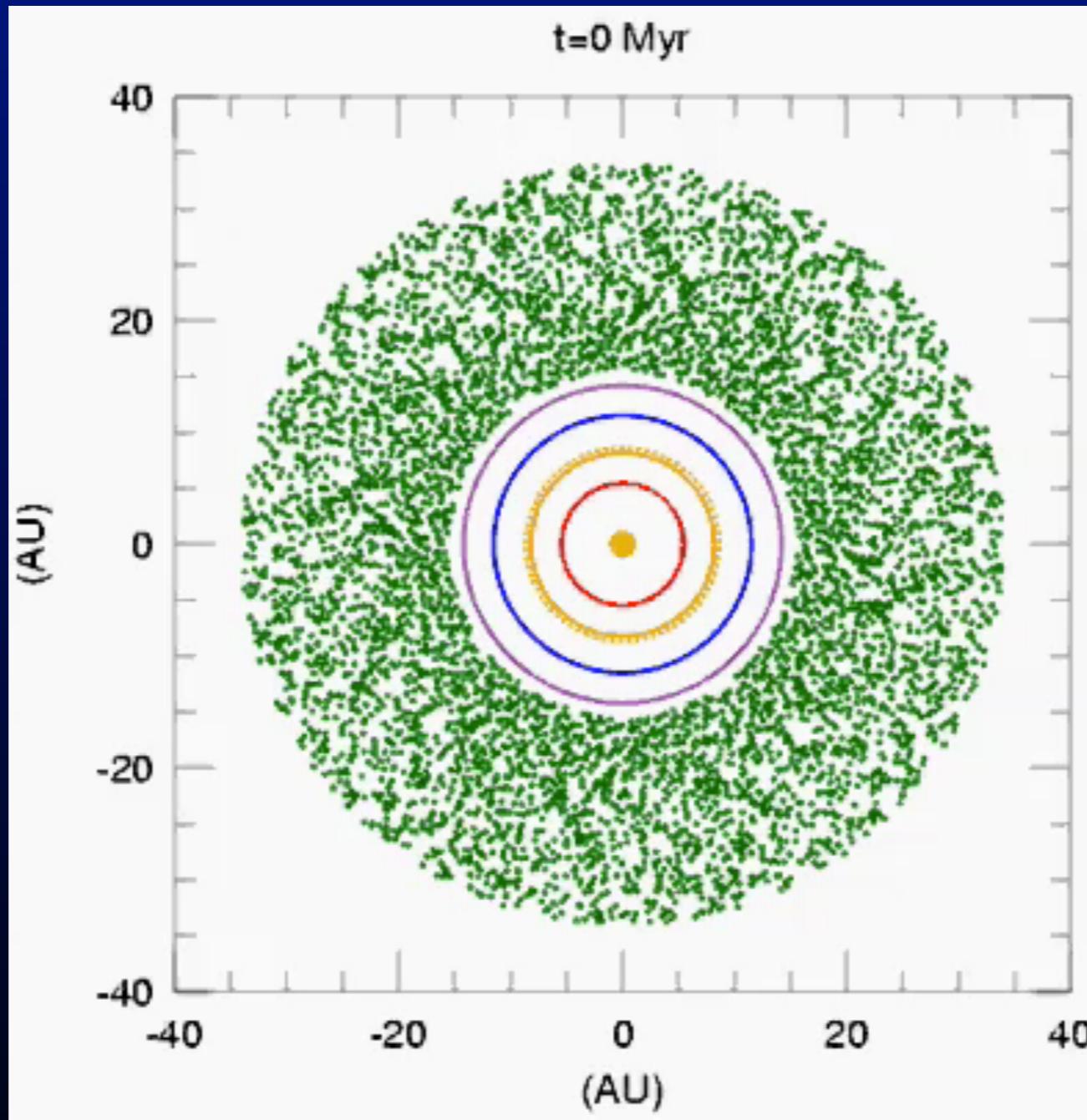
Figure from Chiang et al. (2007)

# Resonant capture



**Animation courtesy of Eugene Chiang**

# The Nice Model



**Animation courtesy of Hal Levison**

# The Nice Model

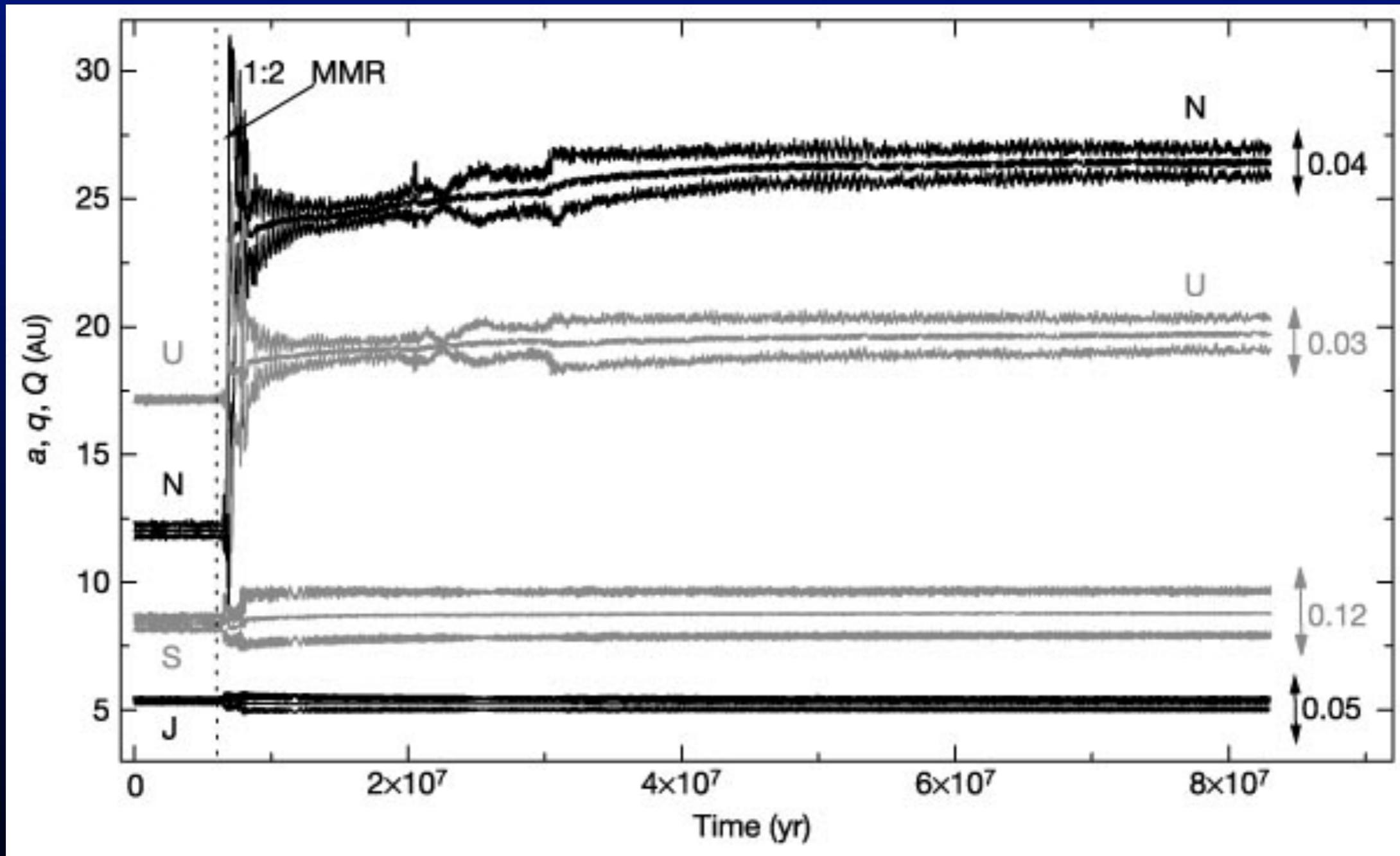
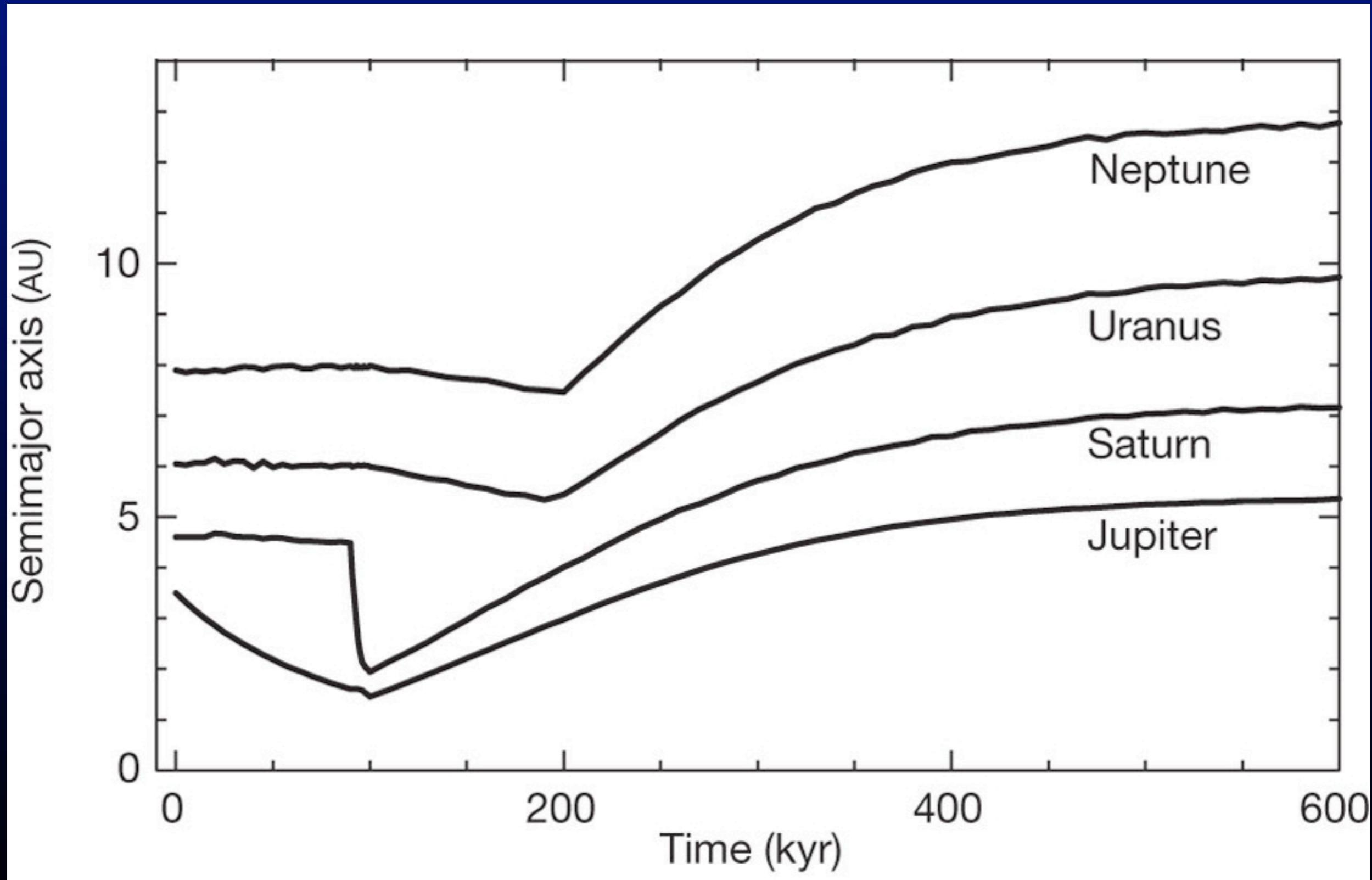


Figure from Tsiganis et al. (2005)

# The “Grand Tack”

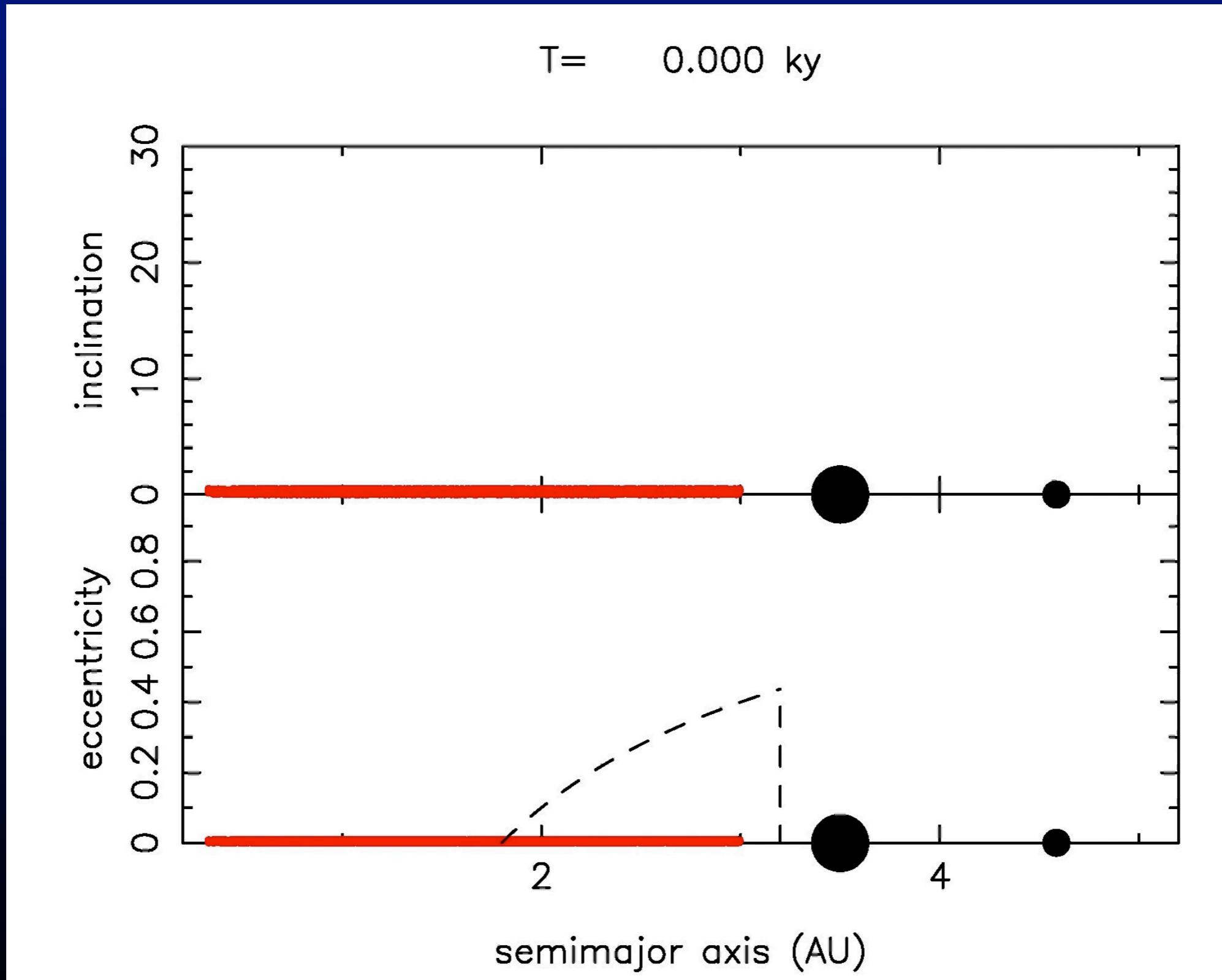
Walsh et al. (2011)



Movies courtesy of Sean Raymond

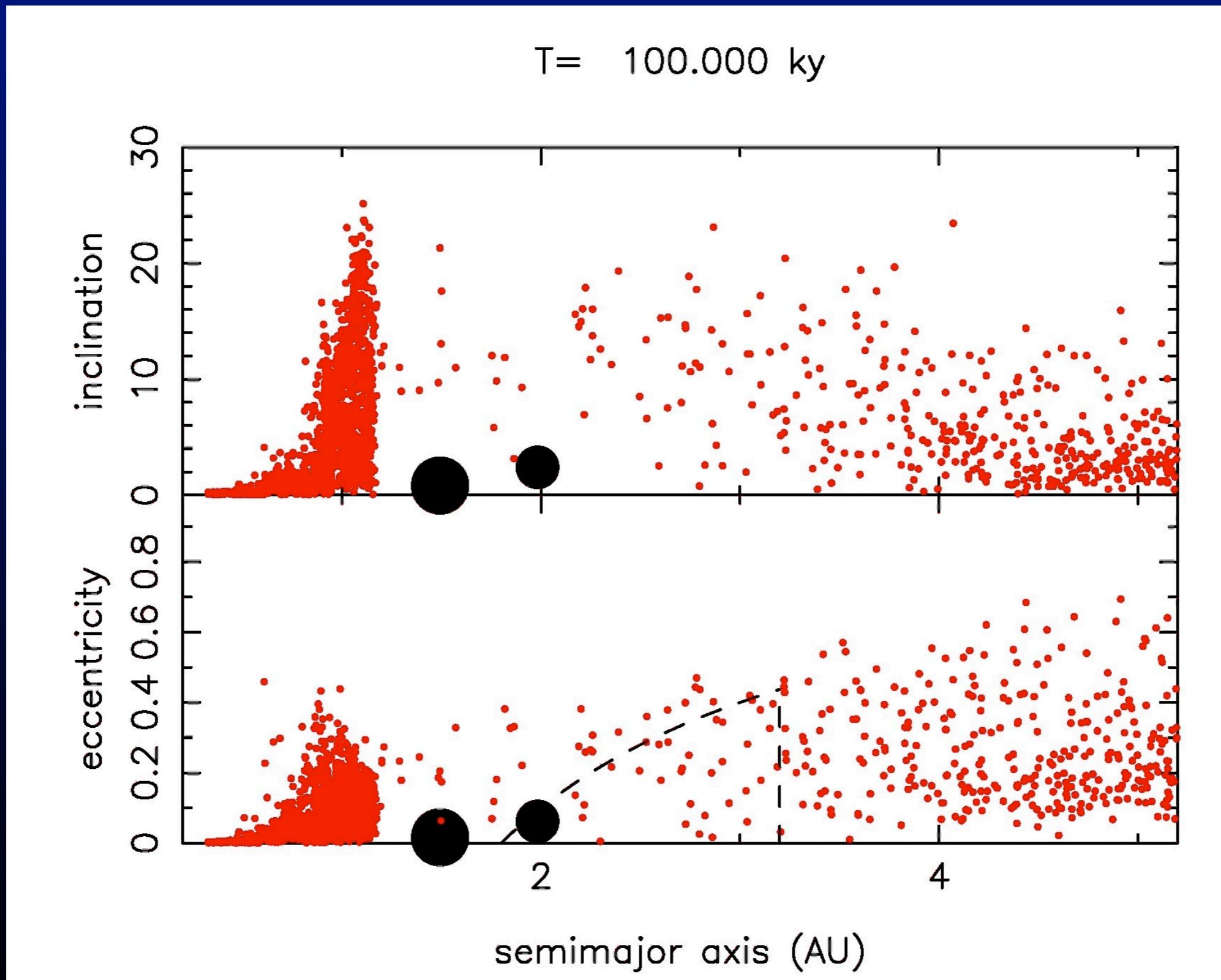
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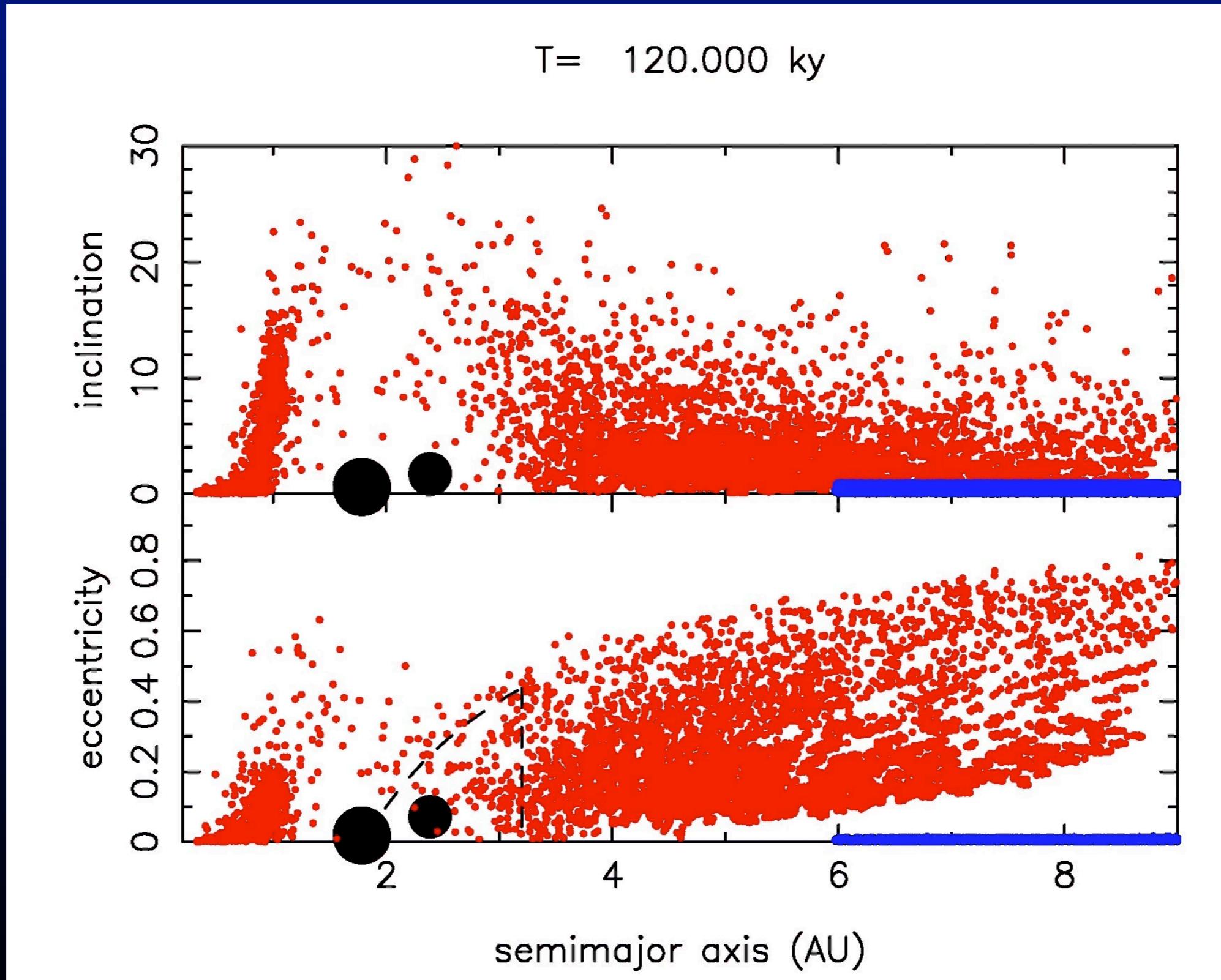
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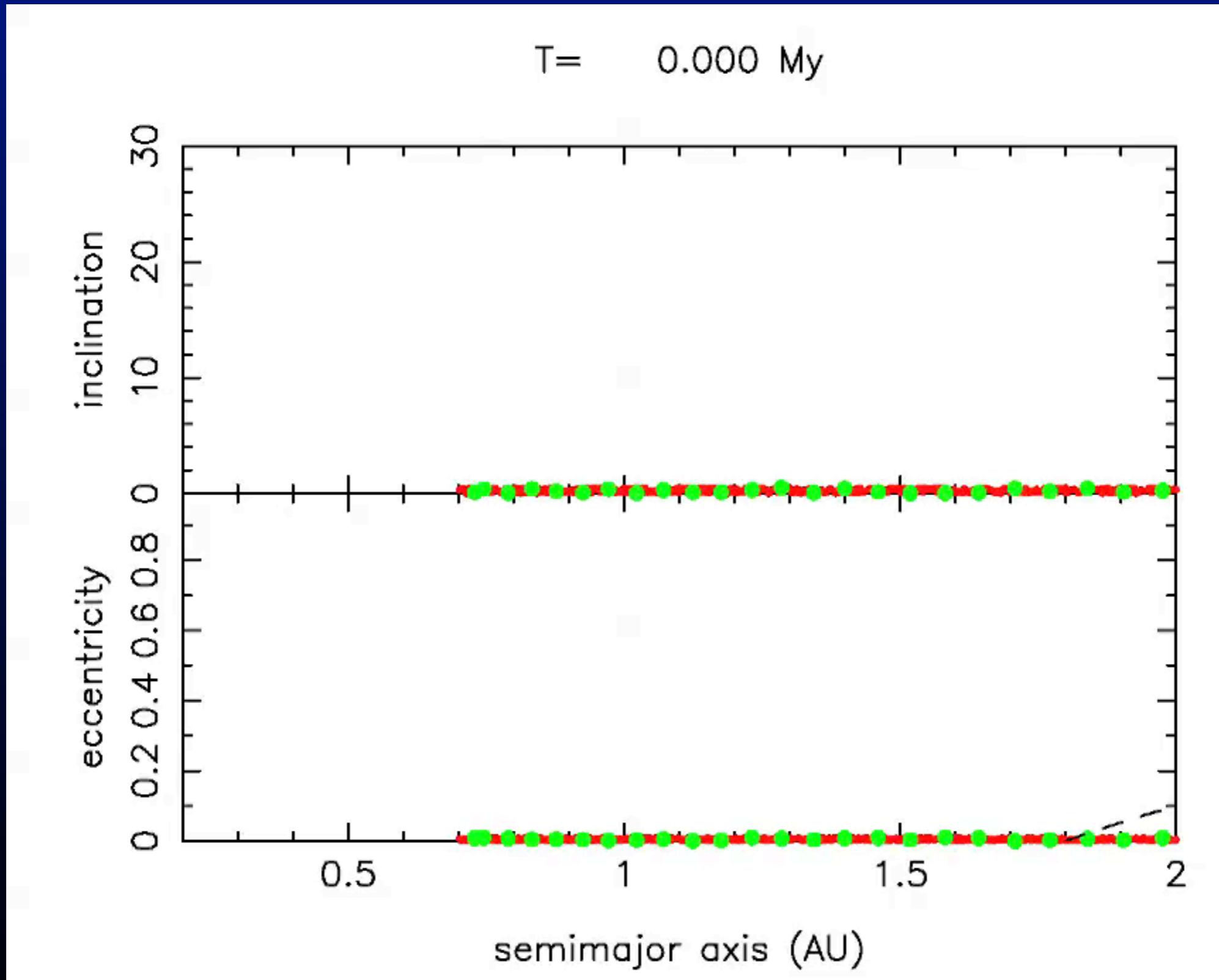
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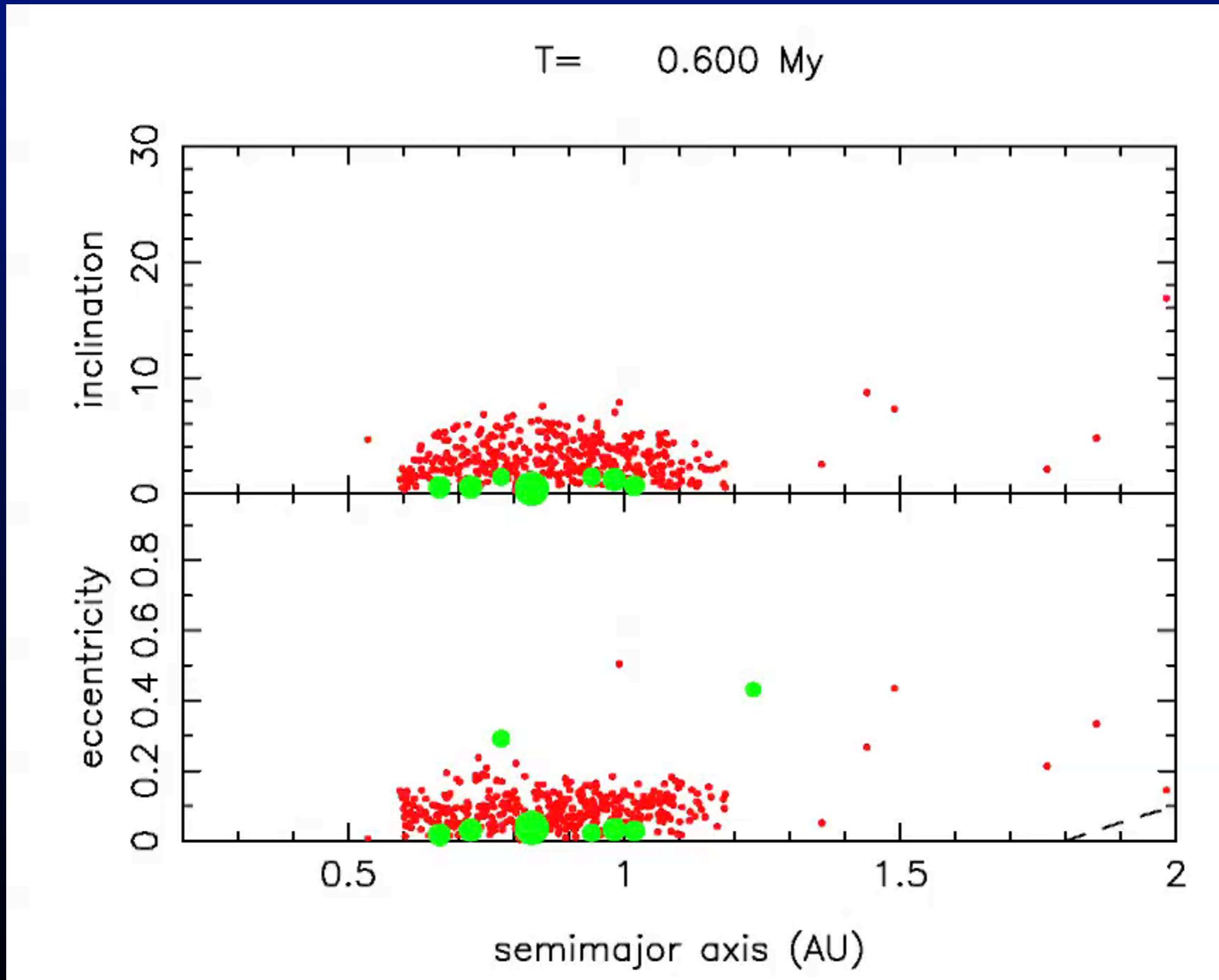
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