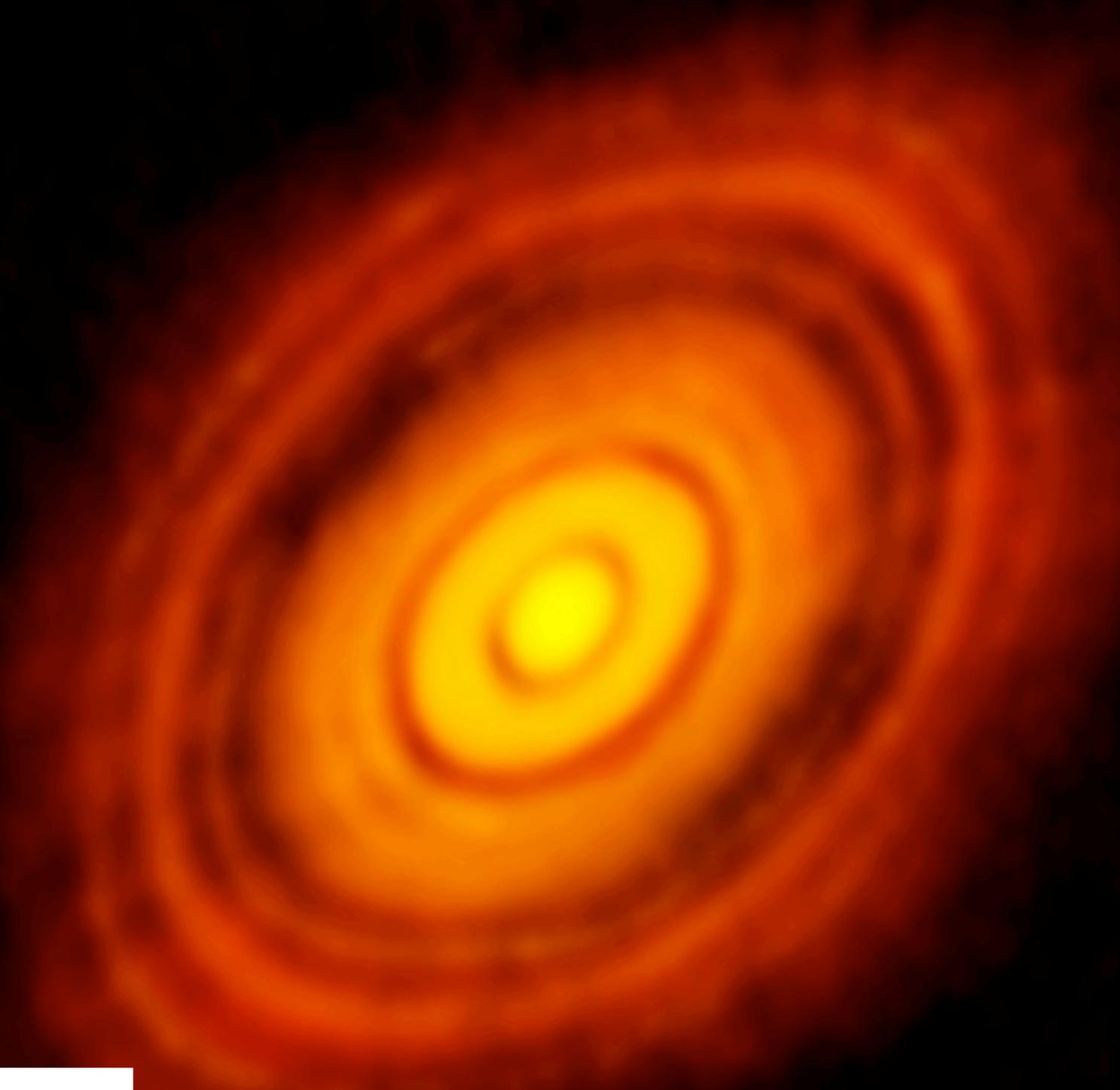


# Formation of Planetary Systems

## Lecture 2 - Protoplanetary discs

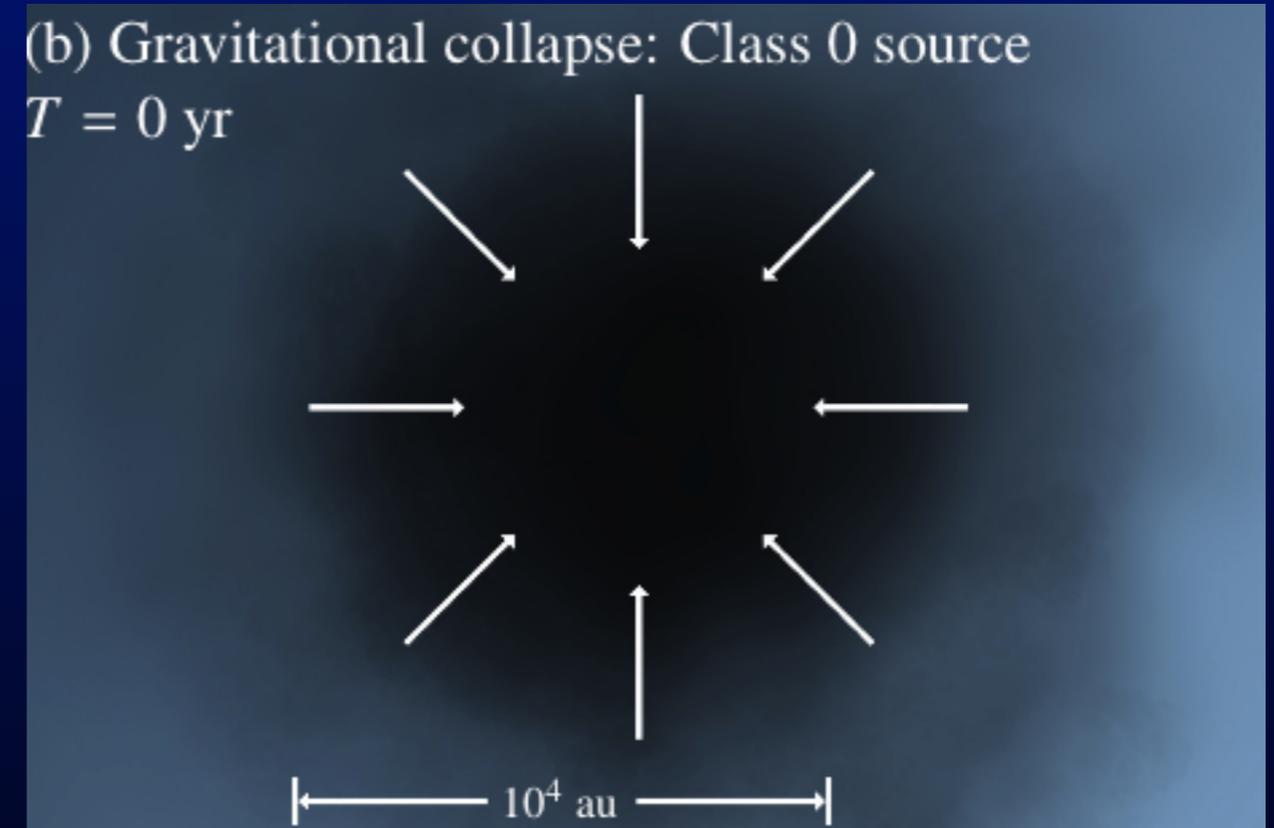
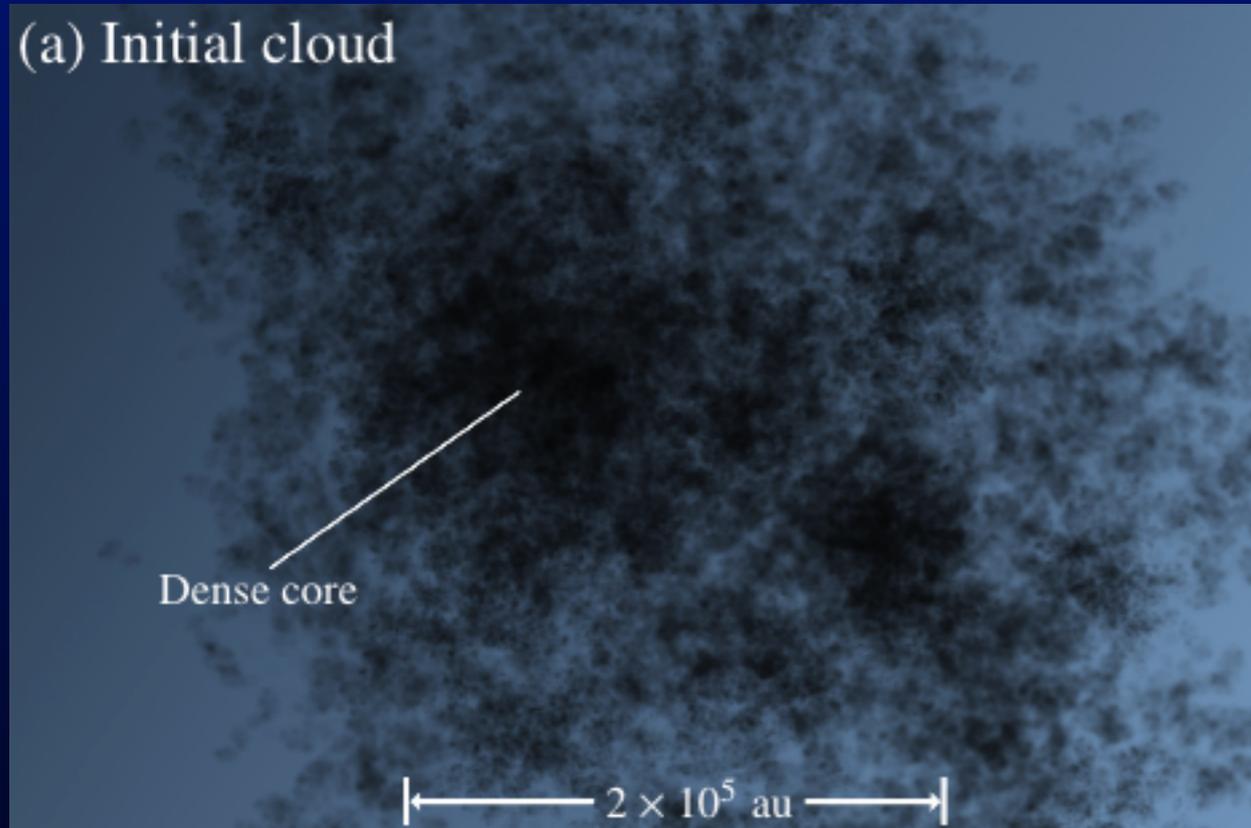


# Course Outline

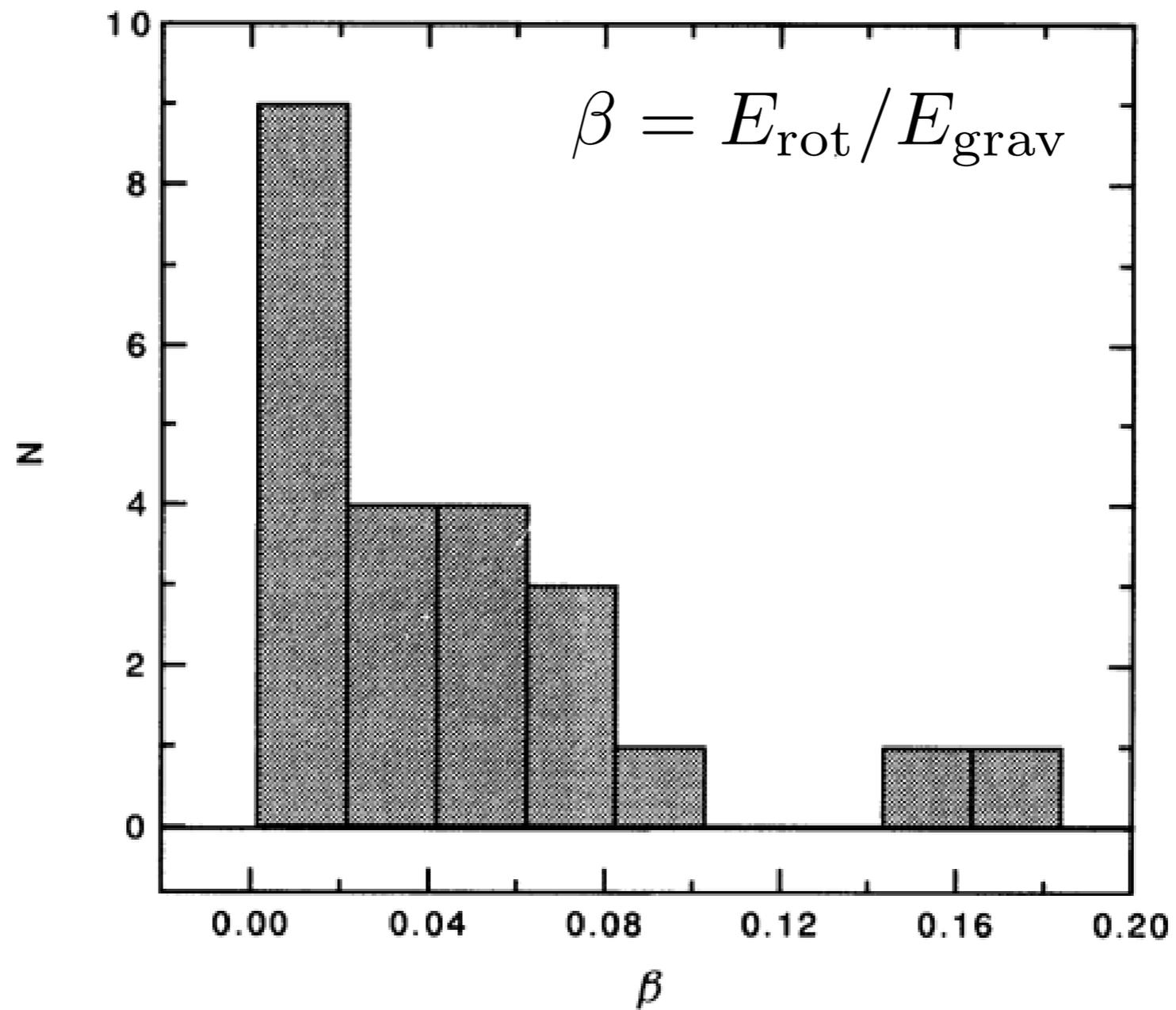
- 5 Lectures, 2 hours each (with a break in the middle!).
  - 1) Observations of planetary systems
  - 2) Protoplanetary discs
  - 3) Dust dynamics & planetesimal formation
  - 4) Planet formation
  - 5) Planetary dynamics
- Notes for each lecture will be placed on the course home page *in advance* - you may find it useful to annotate these as we go.
- These slides will also be posted online.
- Textbooks: Armitage - *Astrophysics of planet formation* (CUP).  
*Protostars & Planets* series (V - 2007; VI - 2014)

# Gravitational collapse

Figures from Alex Dunhill (PhD thesis, 2013), after Shu et al. (1987)



# Measuring rotation

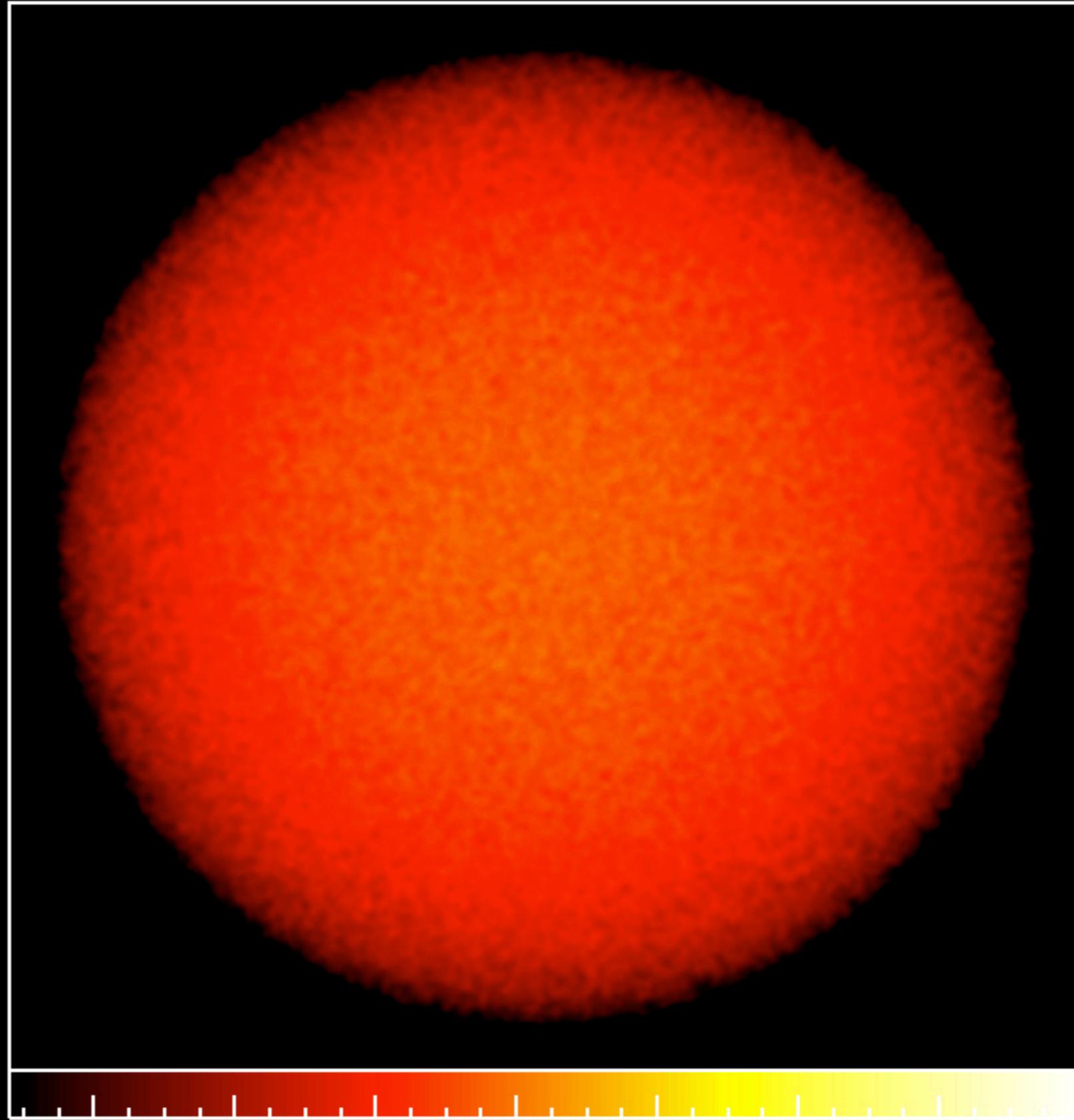


**Goodman et al. (1993)**



Dimensions: 82500. AU

Time: 0. yr



-1.4

-1.2

-1.0

-0.8

-0.6

-0.4

-0.2

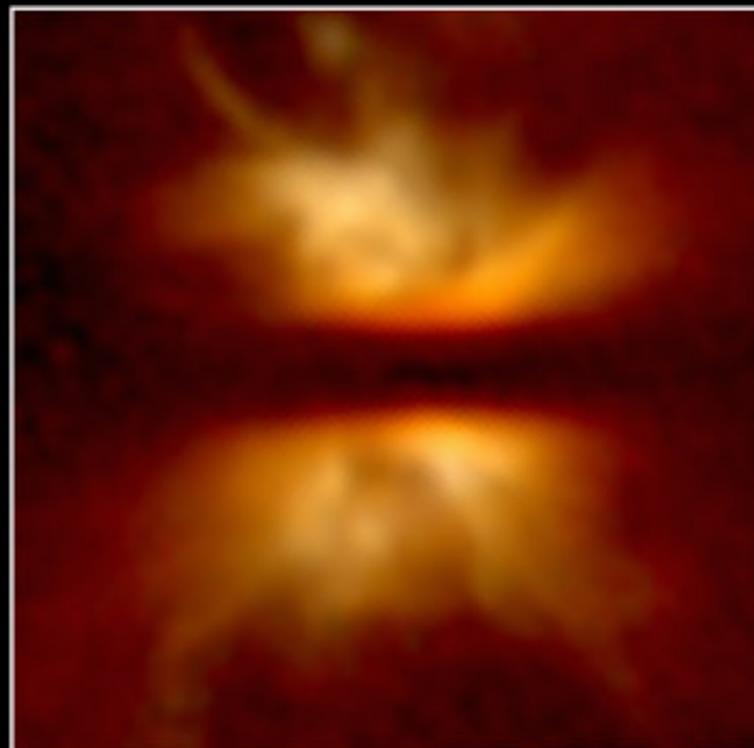
0.0

Log Column Density [ $\text{g}/\text{cm}^2$ ]

Matthew Bate

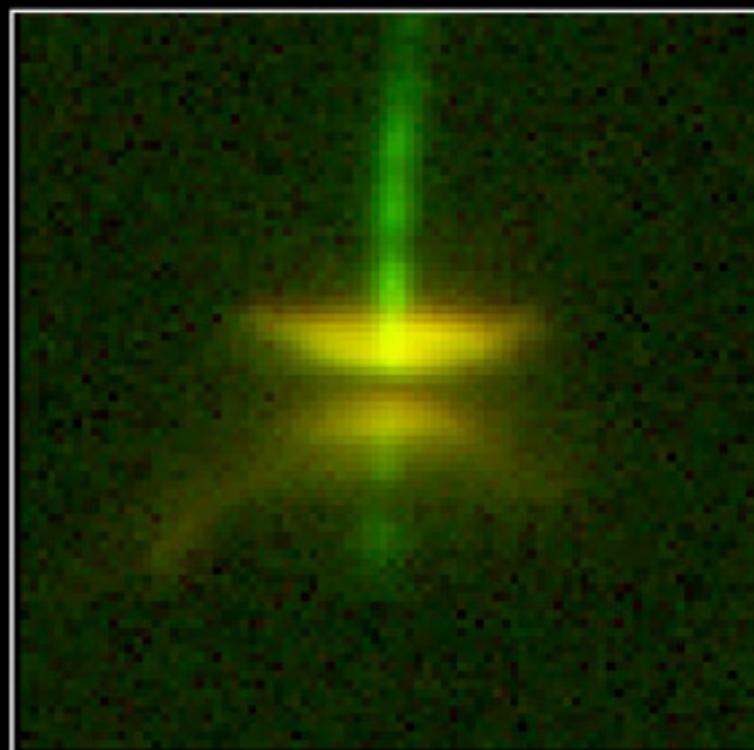
**Bate et al. (2002, 2003)**

**IRAS 04302+2247**



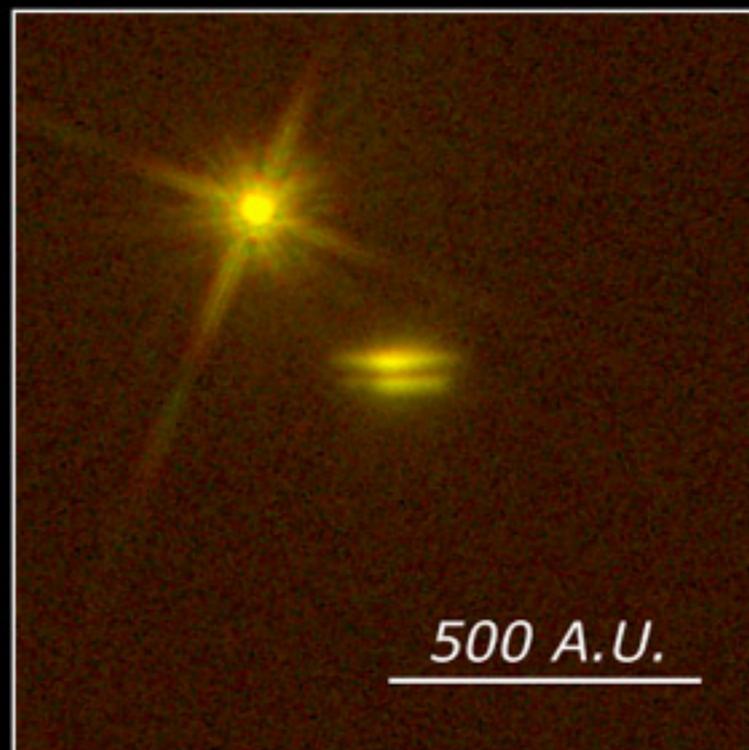
**NICMOS**

**Orion 114-426**



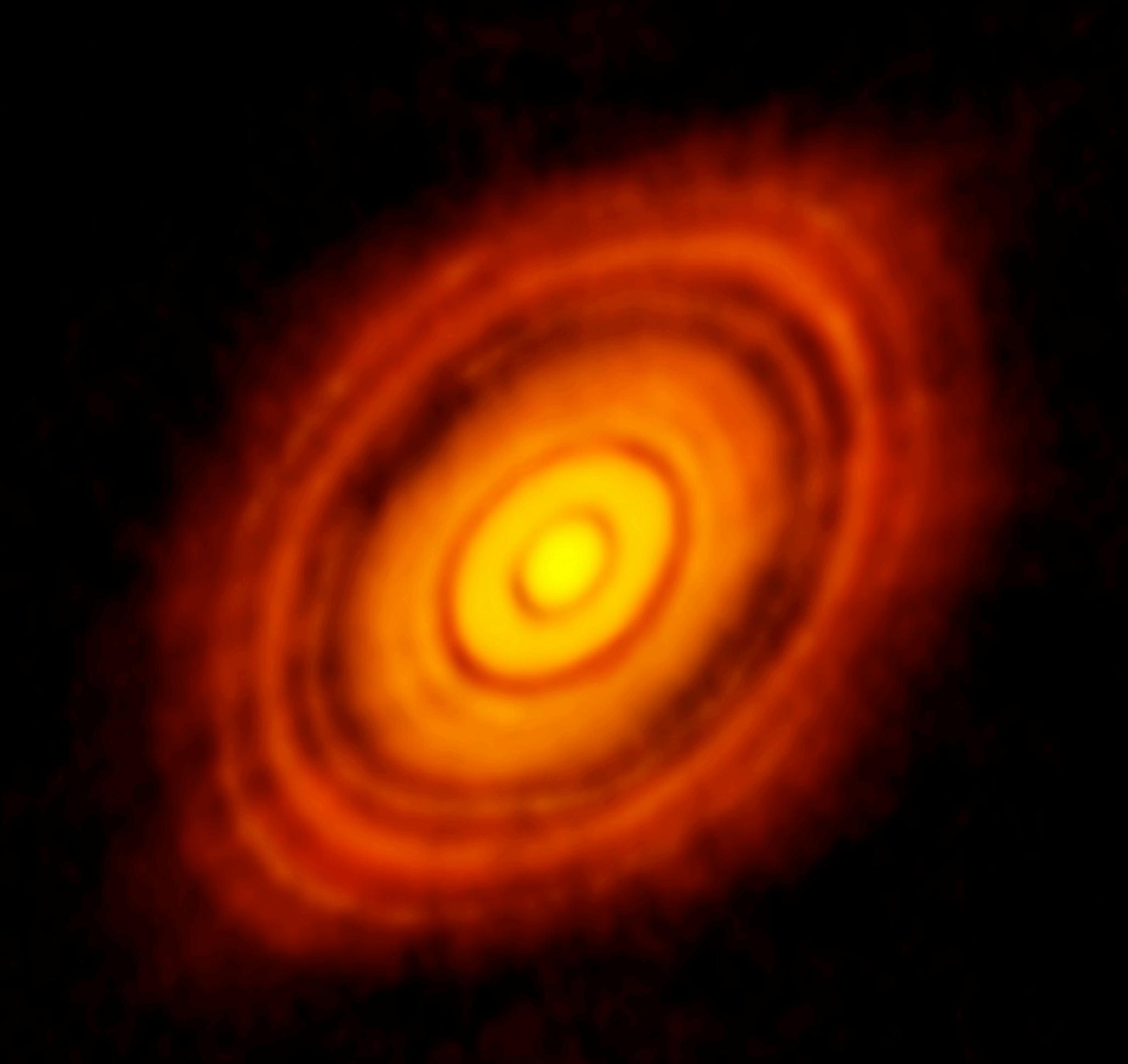
**WFPC2**

**HH 30**

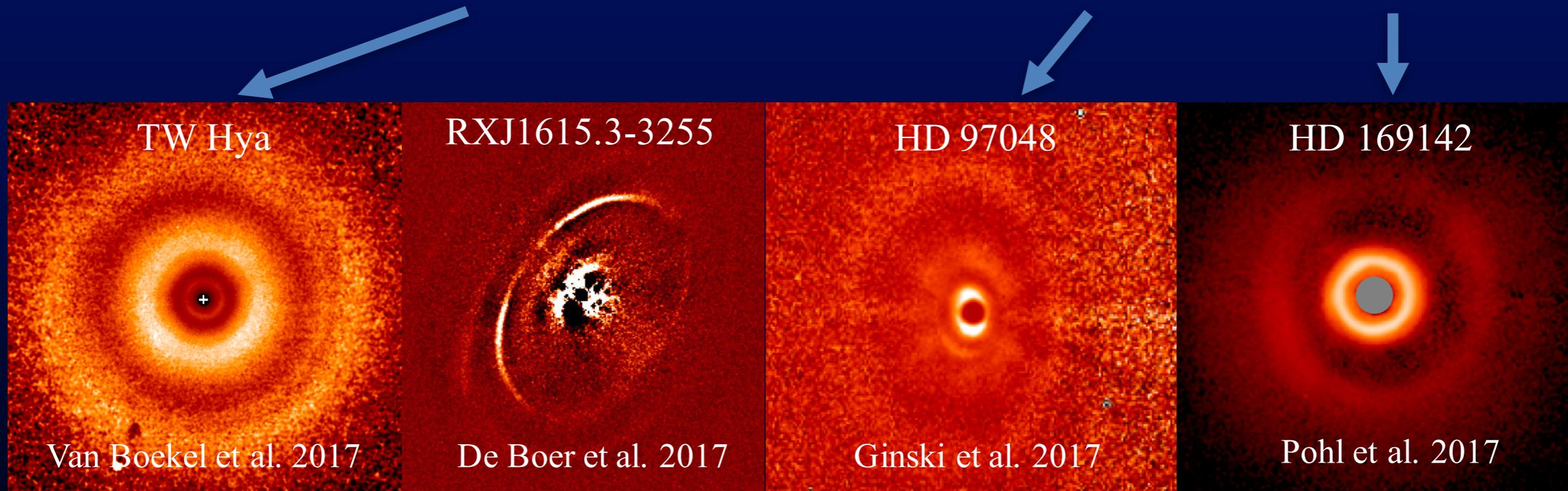
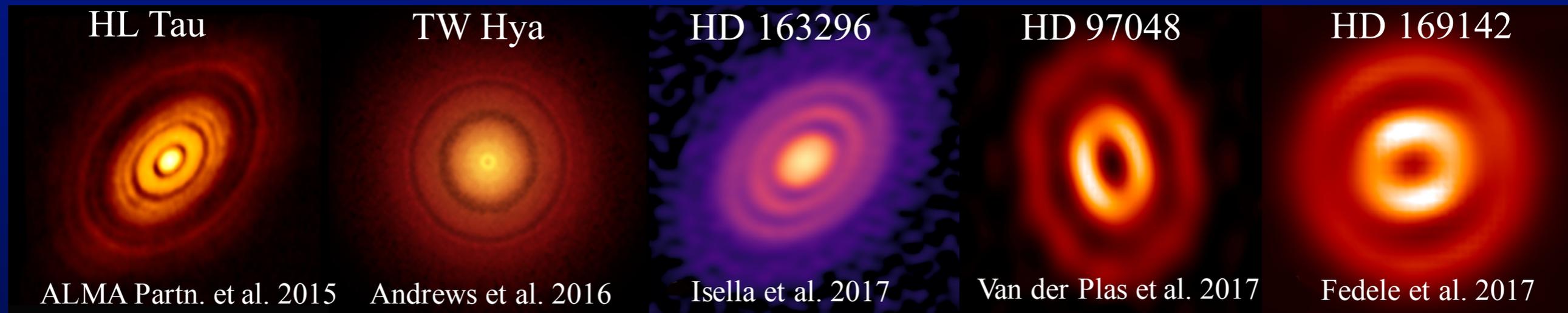


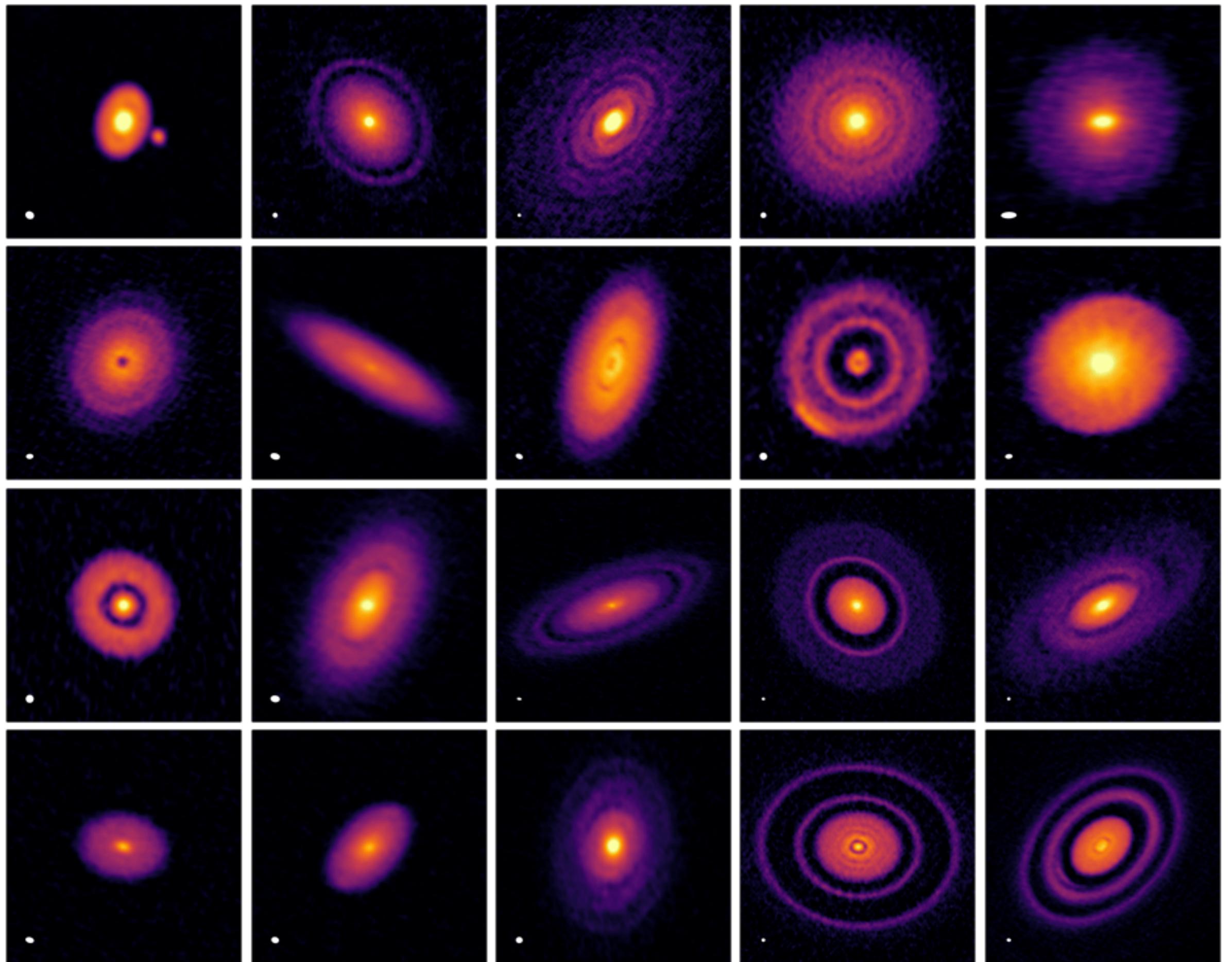
**HK Tau/c**

500 A.U.

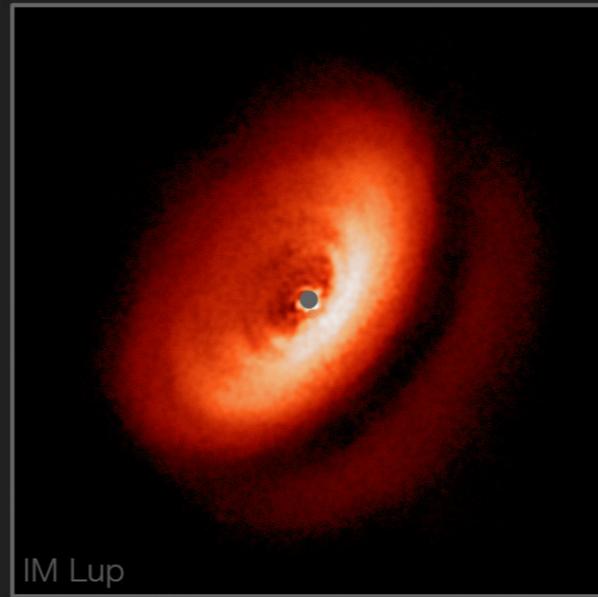
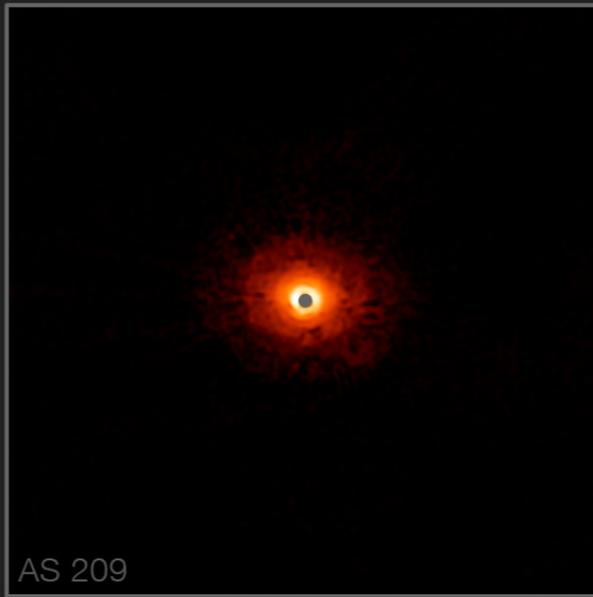
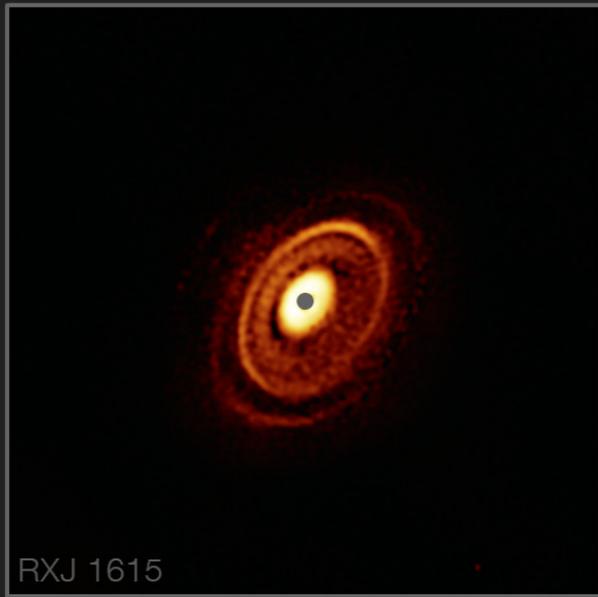
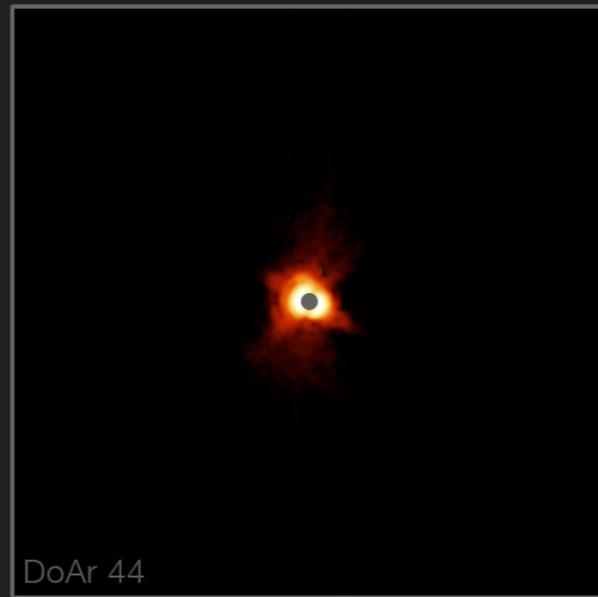
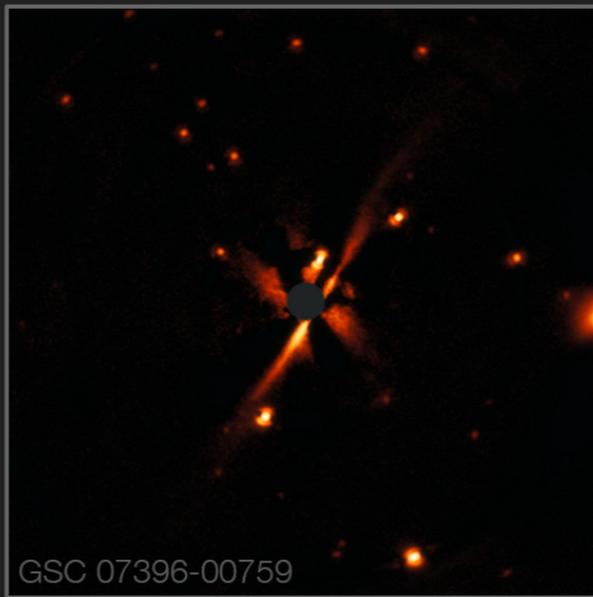
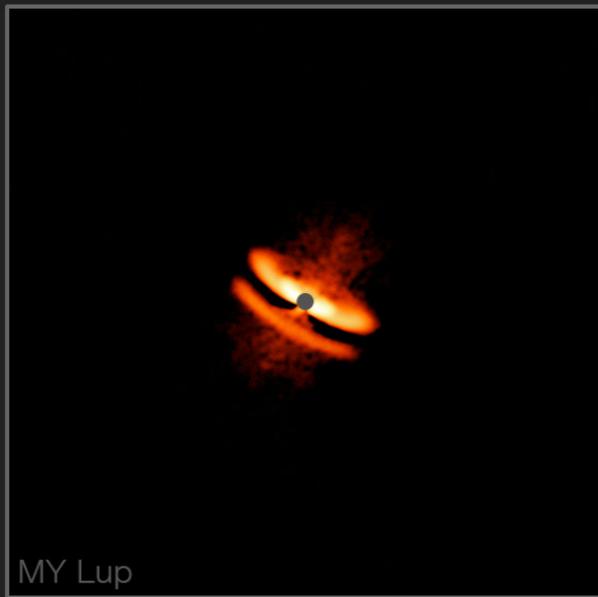
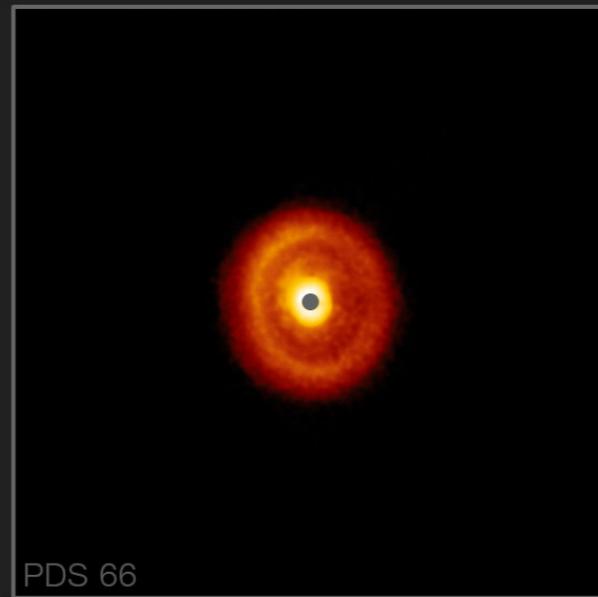
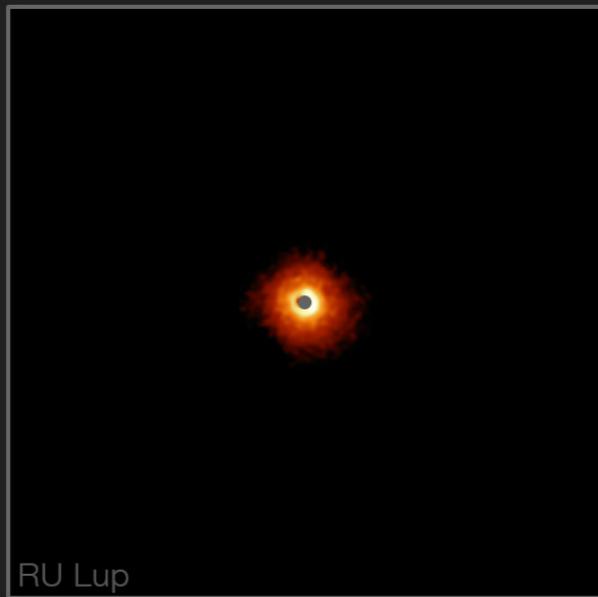


**HL Tau @ 1.3mm: ALMA partnership (2015)**



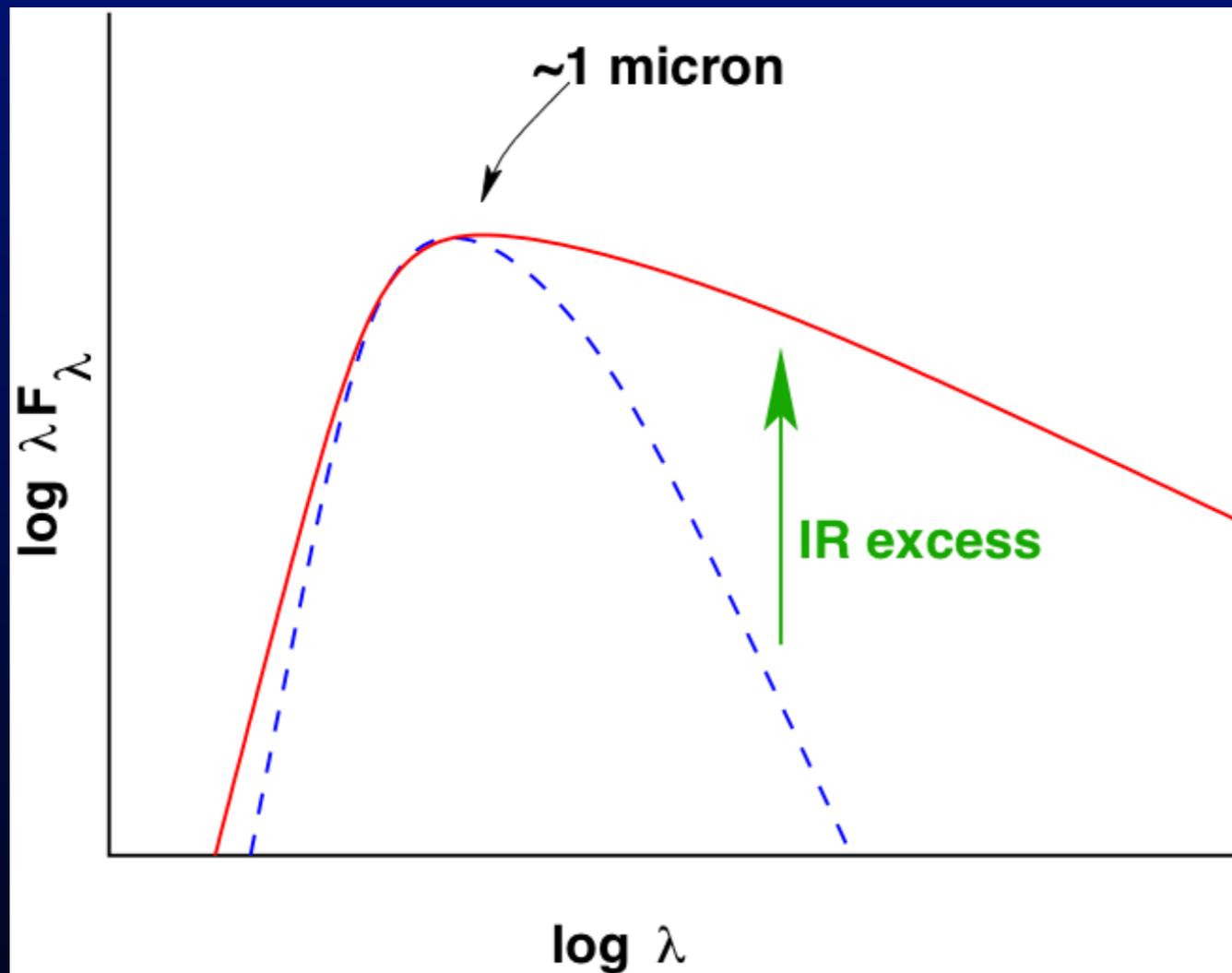


**ALMA “DSHARP” survey; Andrews et al. (2018)**



1"

# SED Classification Scheme



Armitage (2007)

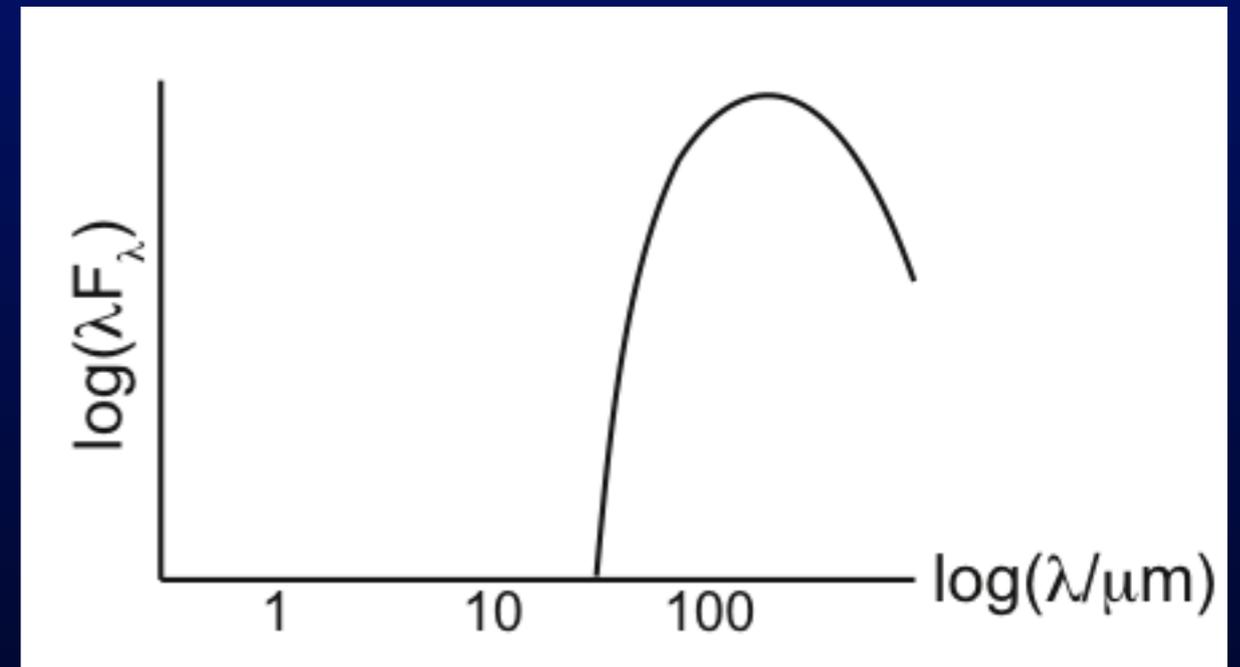
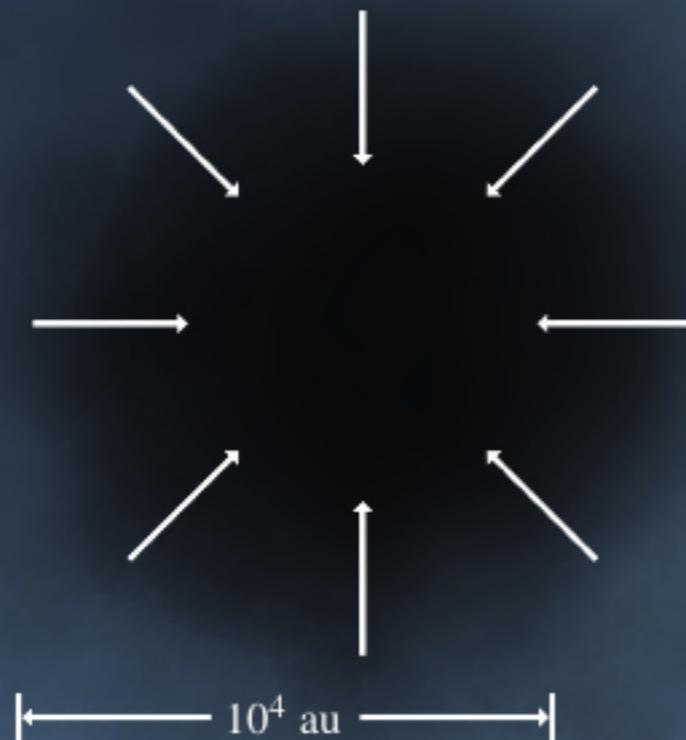
$$\alpha_{\text{IR}} = \frac{d \log (\lambda F_\lambda)}{d \log \lambda}$$

# SED Classification Scheme

Figures from Alex Dunhill (PhD thesis, 2013) & Armitage (2010)

(b) Gravitational collapse: Class 0 source

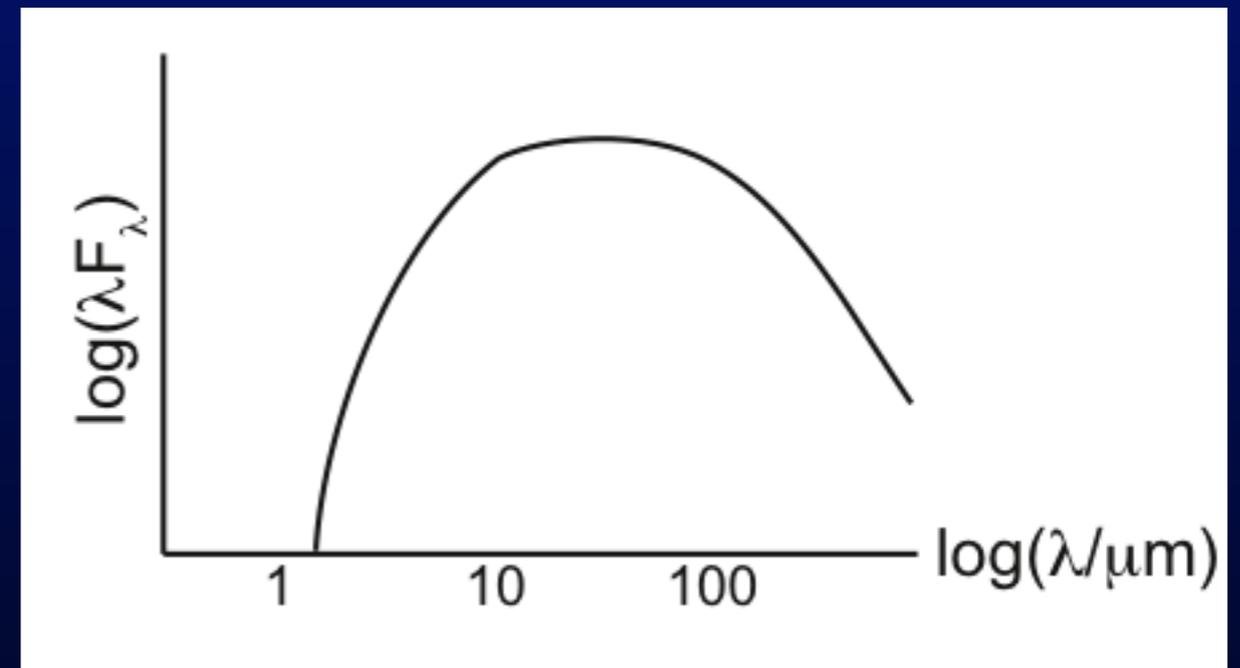
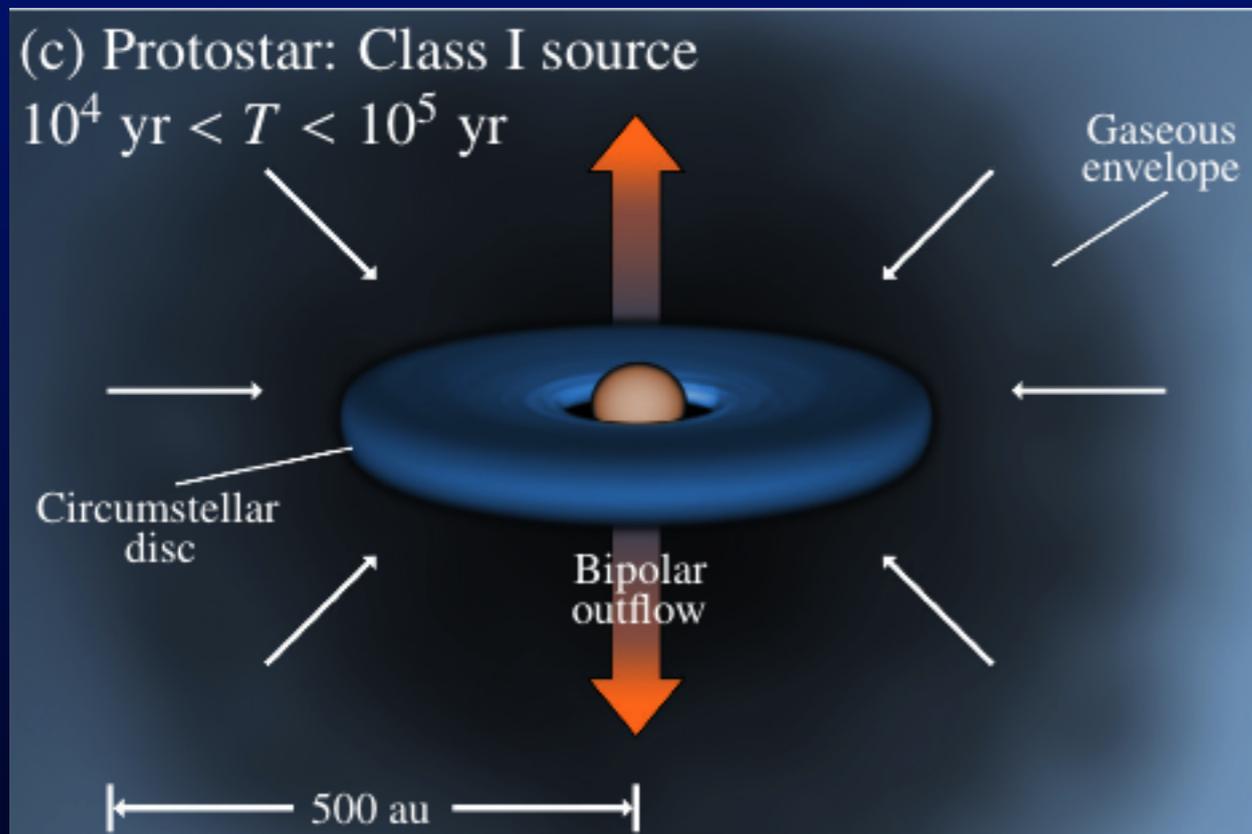
$T = 0$  yr



Class 0: sub-mm sources, no detectable IR emission

# SED Classification Scheme

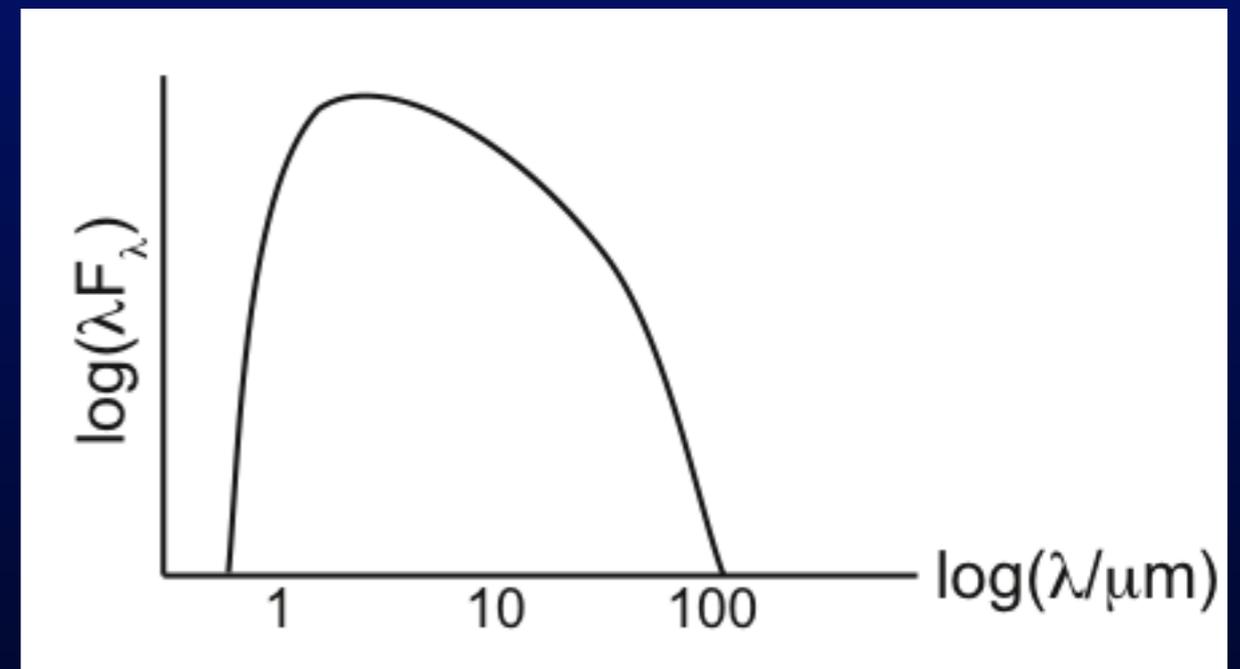
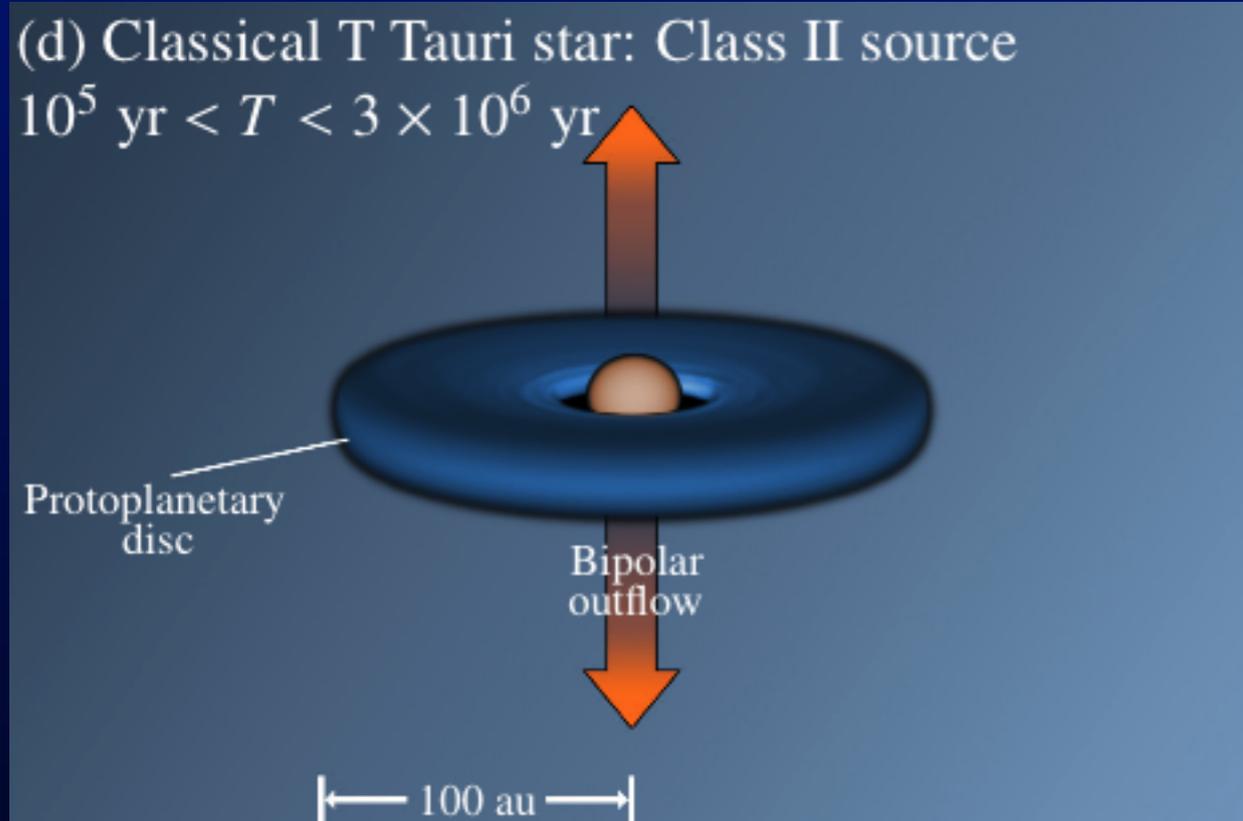
Figures from Alex Dunhill (PhD thesis, 2013) & Armitage (2010)



Class I:  $\alpha_{\text{IR}} \gtrsim 0.0$

# SED Classification Scheme

Figures from Alex Dunhill (PhD thesis, 2013) & Armitage (2010)

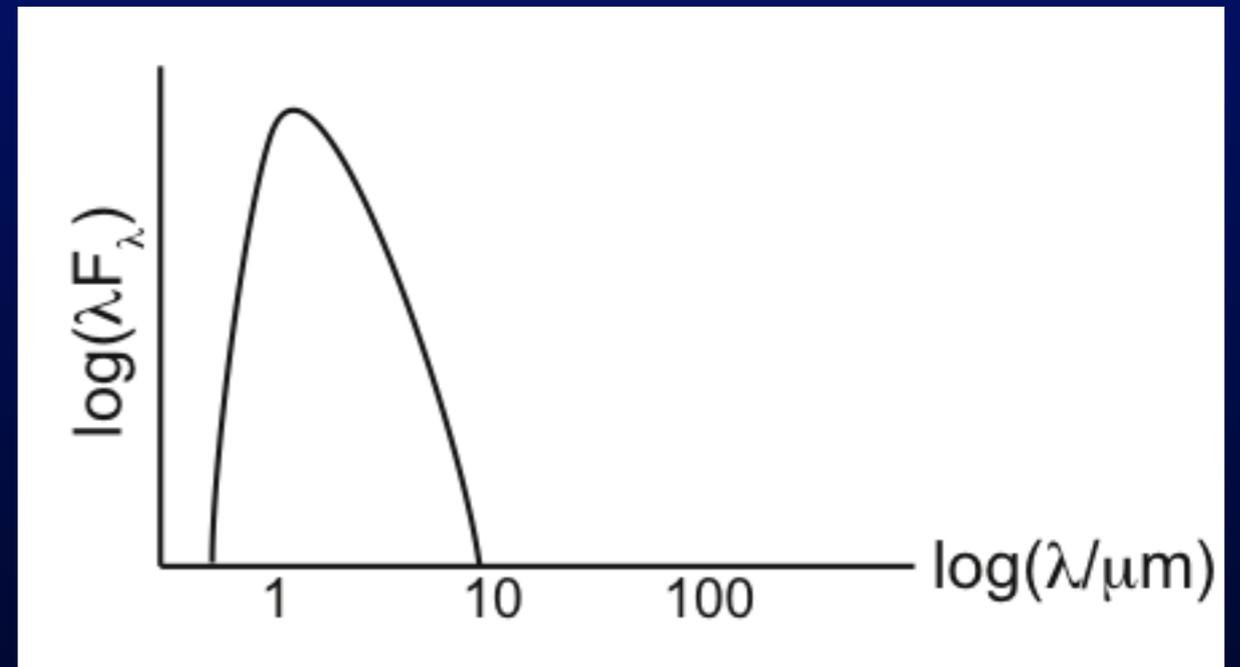
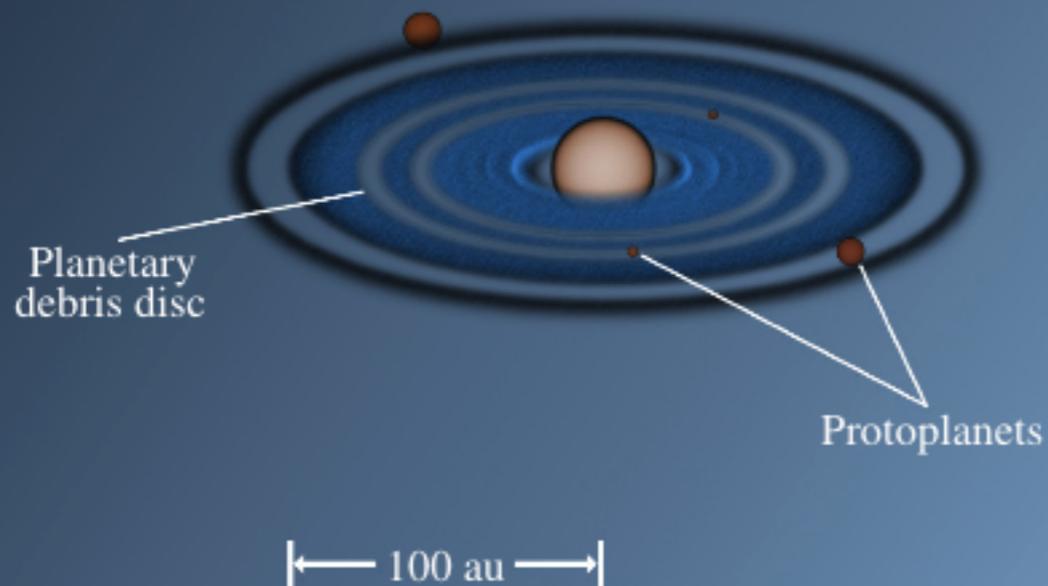


$$\text{Class II: } -1.5 \lesssim \alpha_{\text{IR}} \lesssim 0.0$$

# SED Classification Scheme

Figures from Alex Dunhill (PhD thesis, 2013) & Armitage (2010)

(e) Weak-lined T Tauri star: Class III source  
 $3 \times 10^5 \text{ yr} < T < 5 \times 10^7 \text{ yr}$

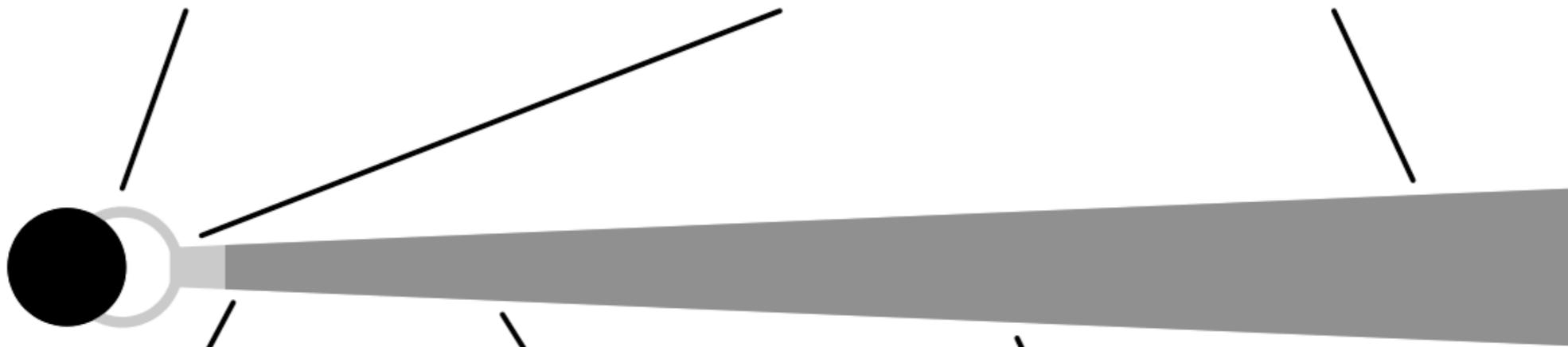


**Class III:**  $\alpha_{\text{IR}} \sim -1.5$

# Observations of protoplanetary discs

**GAS**

UV excess, veiling, broad emission lines  
Hot gas emission lines CO (ro-vib), H<sub>2</sub>, etc.  
Cold gas emission lines CO (rotational), etc.



near-IR

mid-IR

far-IR

(sub)-mm

$\tau \gg 1$

$\tau \sim 1$

$\tau < 1$

0.1AU

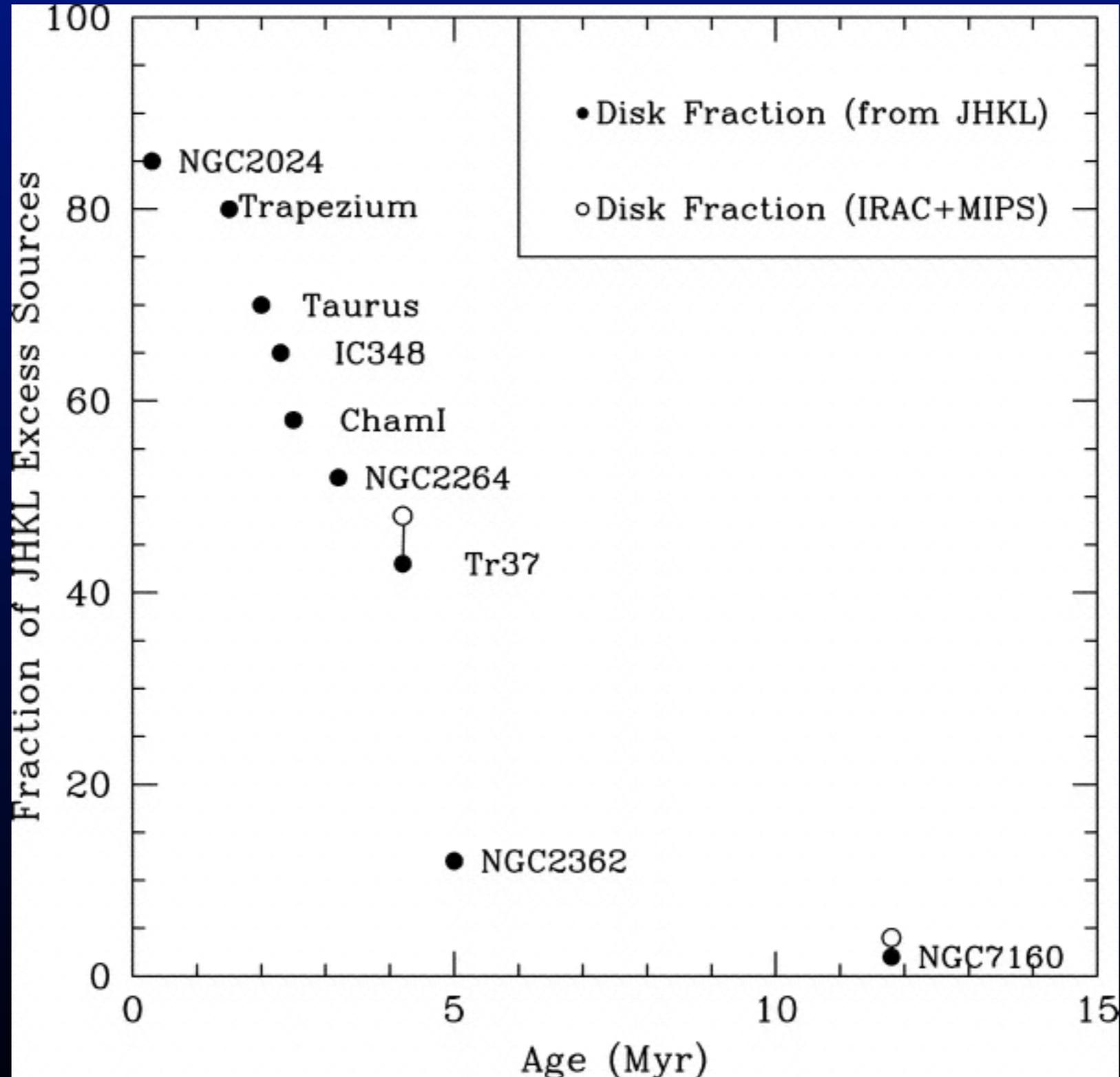
1AU

10AU

100AU

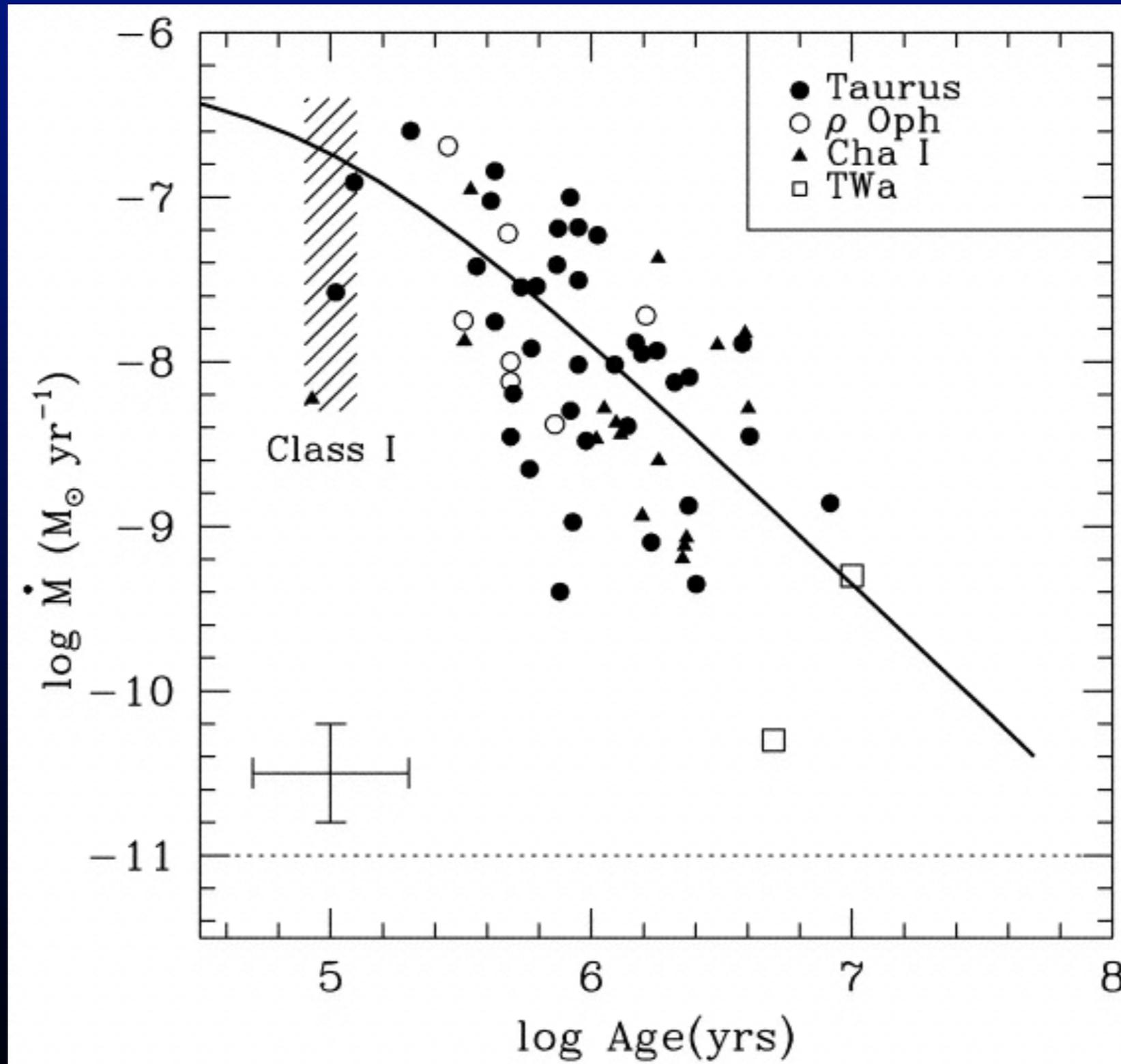
**DUST**

# Disc lifetimes



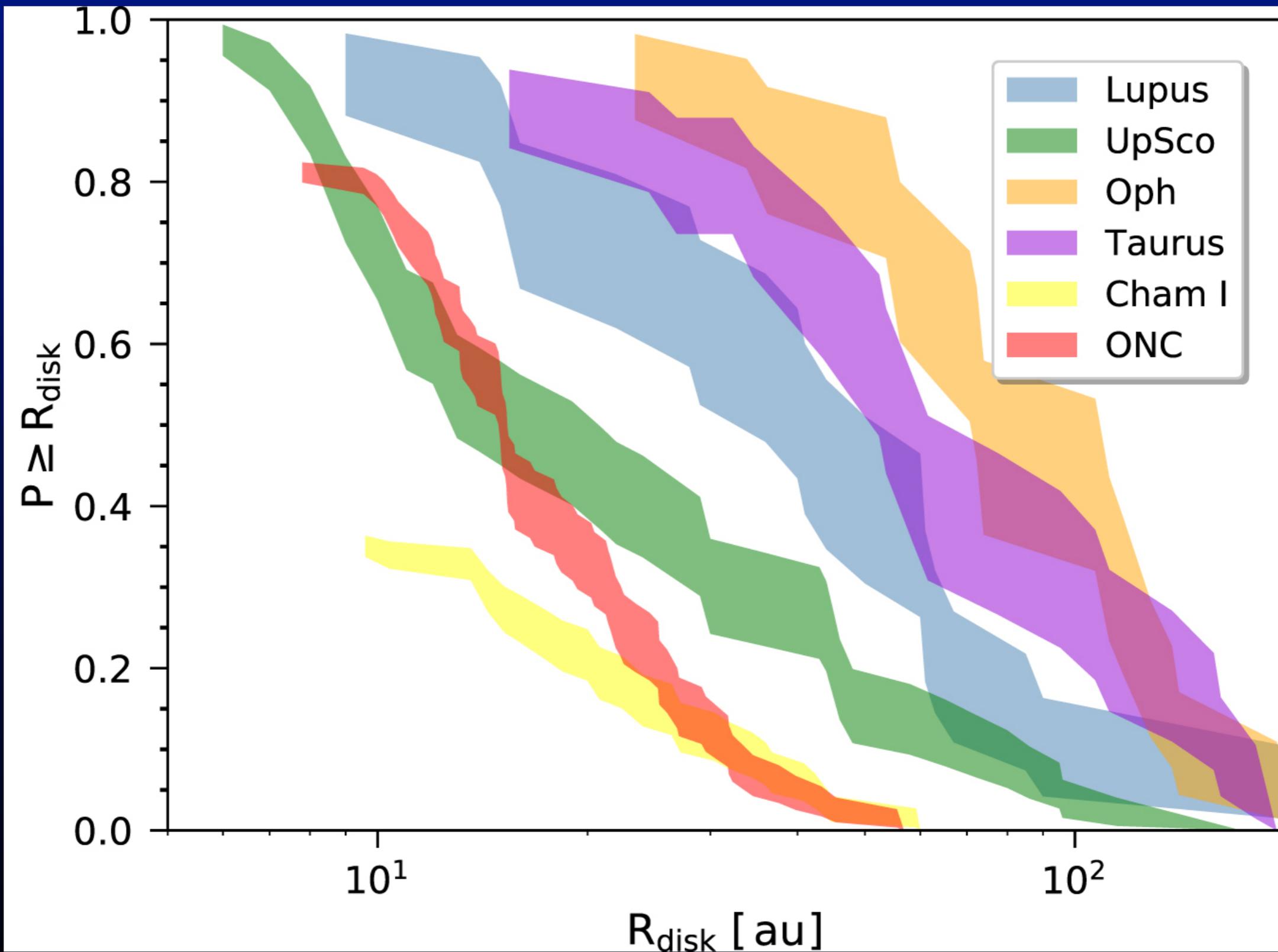
**Sicilia-Aguilar et al. (2006)**

# Accretion rates



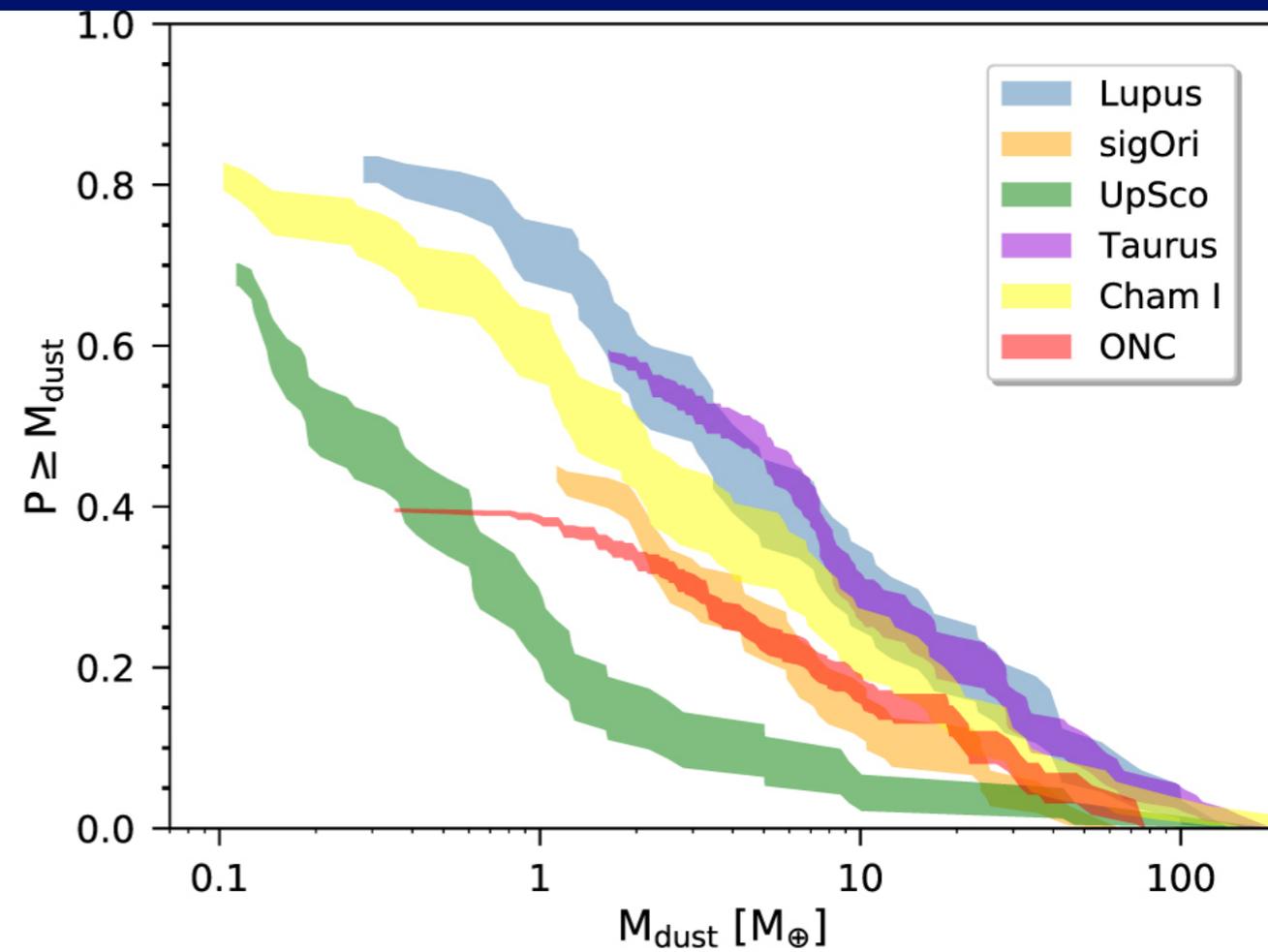
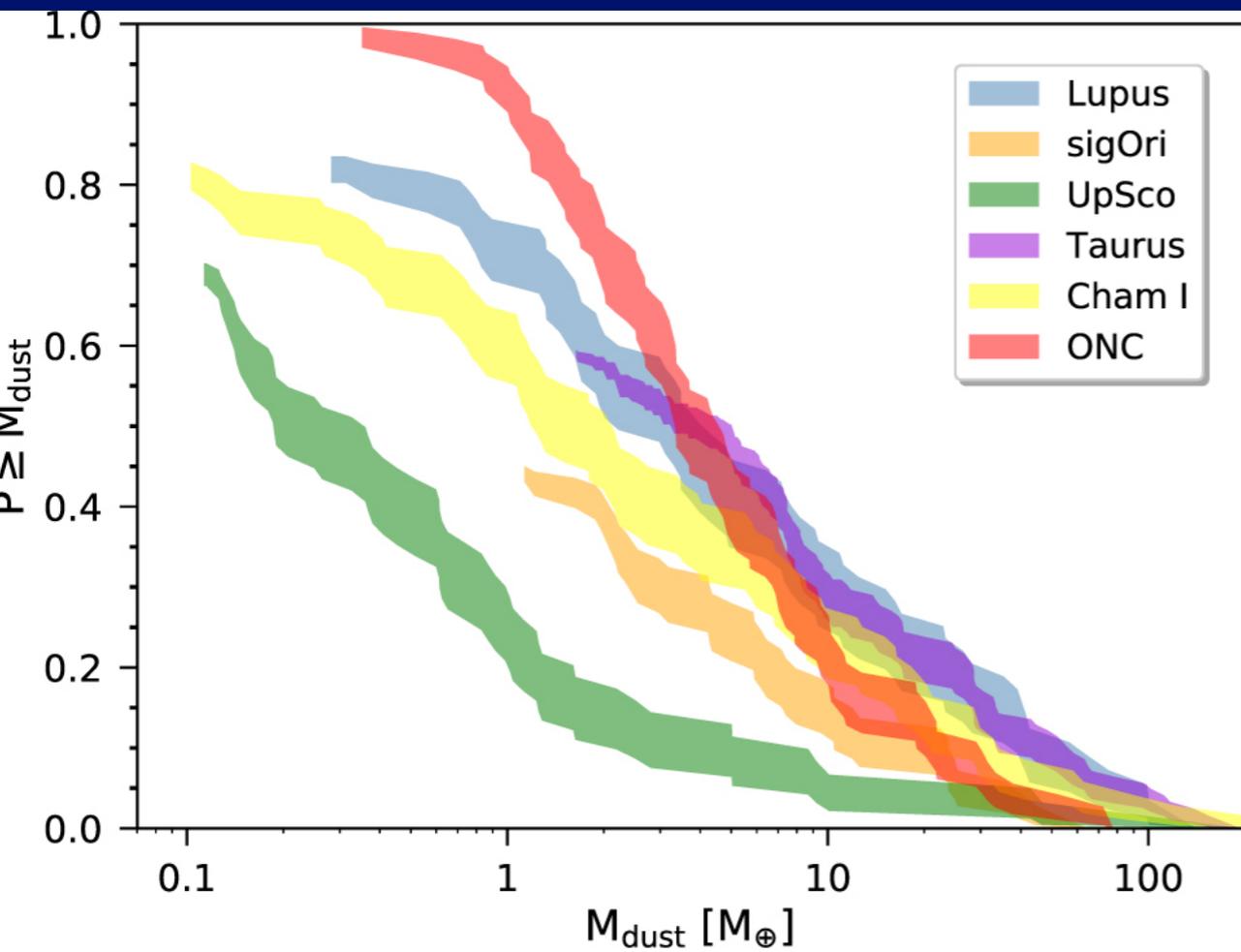
Muzerolle et al. (2000)

# Disc sizes



Data compilation from Eisner et al. (2018)

# Disc masses



**Data compilation from Eisner et al. (2018)**

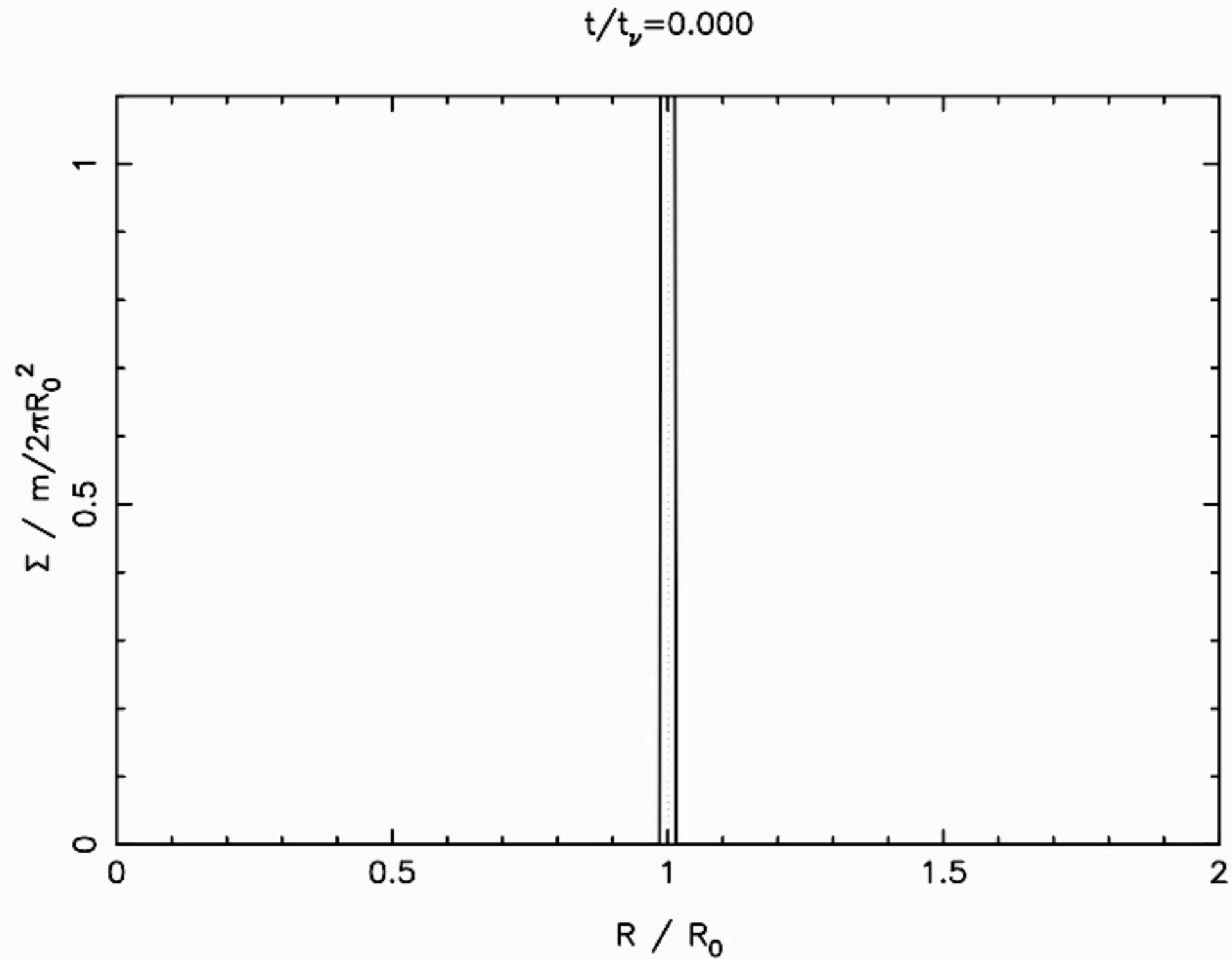
# Observational Summary

- Discs are tens to hundreds of AU in size.
- Disc masses range from  $>0.1 M_{\odot}$  to  $\leq 0.001 M_{\odot}$ .
- Accretion rates span  $>10^{-7} M_{\odot} \text{yr}^{-1}$  to  $\leq 10^{-10} M_{\odot} \text{yr}^{-1}$ .
- Disc lifetimes are  $\sim \text{Myr}$  (gas and dust tracers), with significant scatter.
- Cessation of (gas) accretion roughly simultaneous with (dust) disc clearing.
- Disc lifetimes set a limit on the time-scale for (giant) planet formation.
- Disc observations tell us the typical conditions for planet formation.



# Viscous spreading ring

Pringle (1981)



# Viscous disc similarity solution

Lynden-Bell & Pringle (1974)

$$\nu \propto R^\gamma$$

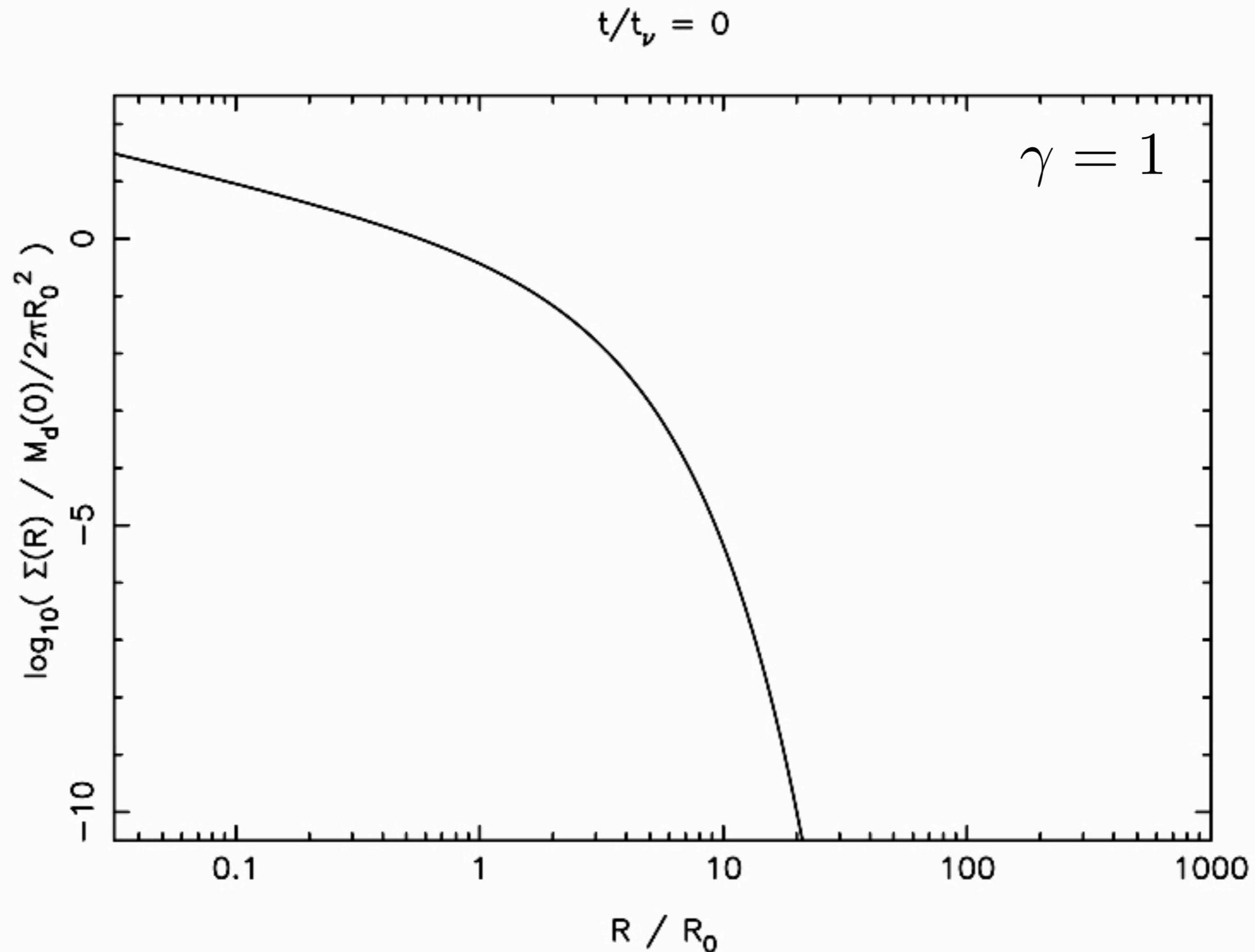
$$\Sigma(R, t) = \frac{M_d(0)(2 - \gamma)}{2\pi R_0^2 r^\gamma} \tau^{\frac{-(5/2 - \gamma)}{2 - \gamma}} \exp\left(-\frac{r^{2 - \gamma}}{\tau}\right)$$

$$r = R/R_0 \quad \tau = t/t_\nu + 1 \quad t_\nu = \frac{R_0^2}{3(2 - \gamma)^2 \nu_0}$$

$$\dot{M}_{acc} = \frac{M_d(0)}{2(2 - \gamma)t_\nu} \tau^{\frac{-(5/2 - \gamma)}{2 - \gamma}}$$

# Viscous disc similarity solution

Lynden-Bell & Pringle (1974)





# Disc stability criteria

- Purely hydrodynamic disc (Rayleigh). Unstable if:

$$\kappa^2 = \frac{2\Omega}{R} \frac{d}{dR} (R^2\Omega) < 0$$

- MHD disc. Unstable if:

$$(\mathbf{k} \cdot \mathbf{u}_A)^2 + \frac{d\Omega^2}{d \ln R} < 0$$

- Alfvén velocity:

$$u_A = \sqrt{B^2 / 4\pi\rho}$$

- In limit  $B \rightarrow 0$  (weak B-field), unstable if:

$$\frac{d\Omega^2}{d \ln R} < 0$$

# The magnetorotational instability

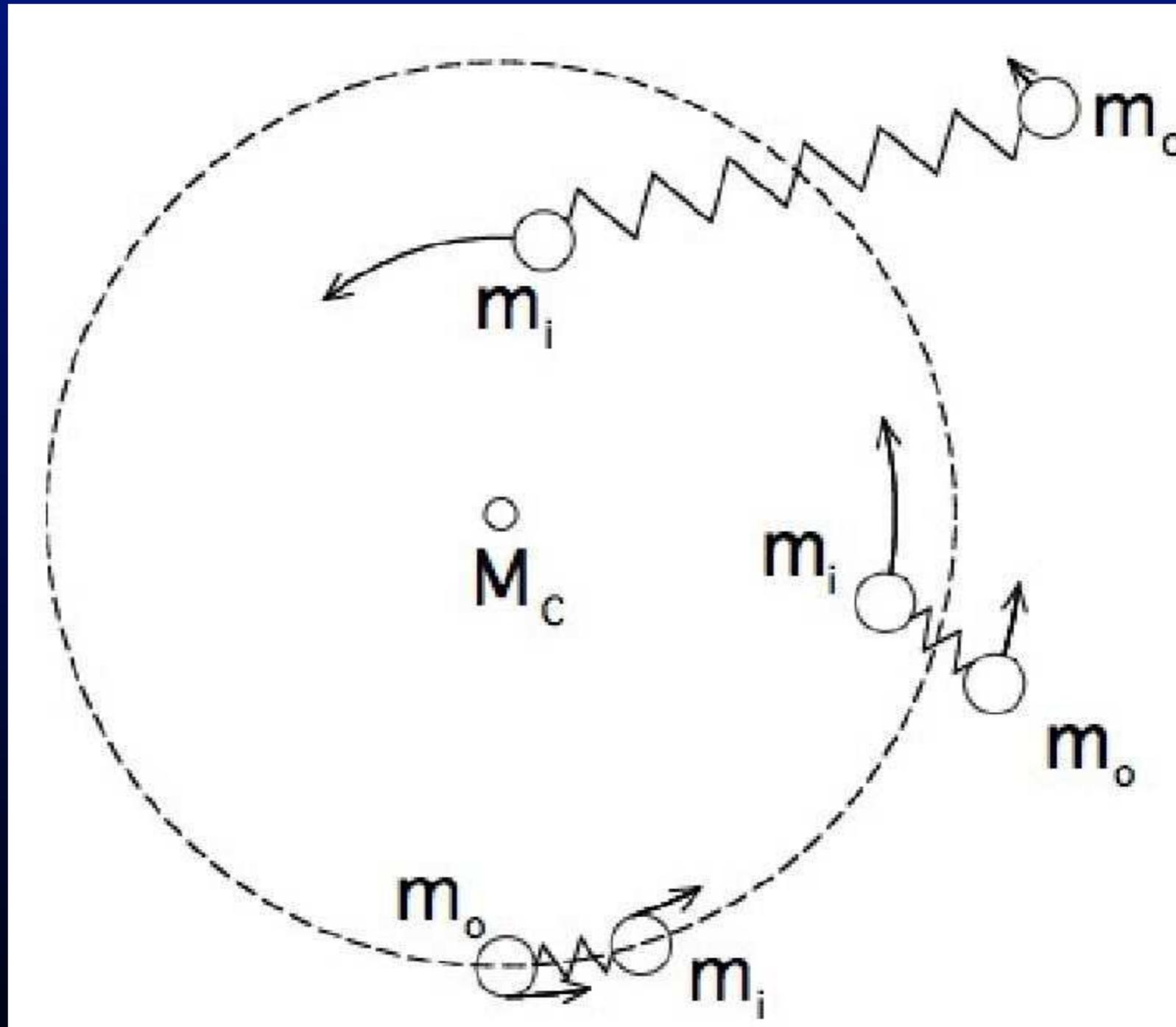
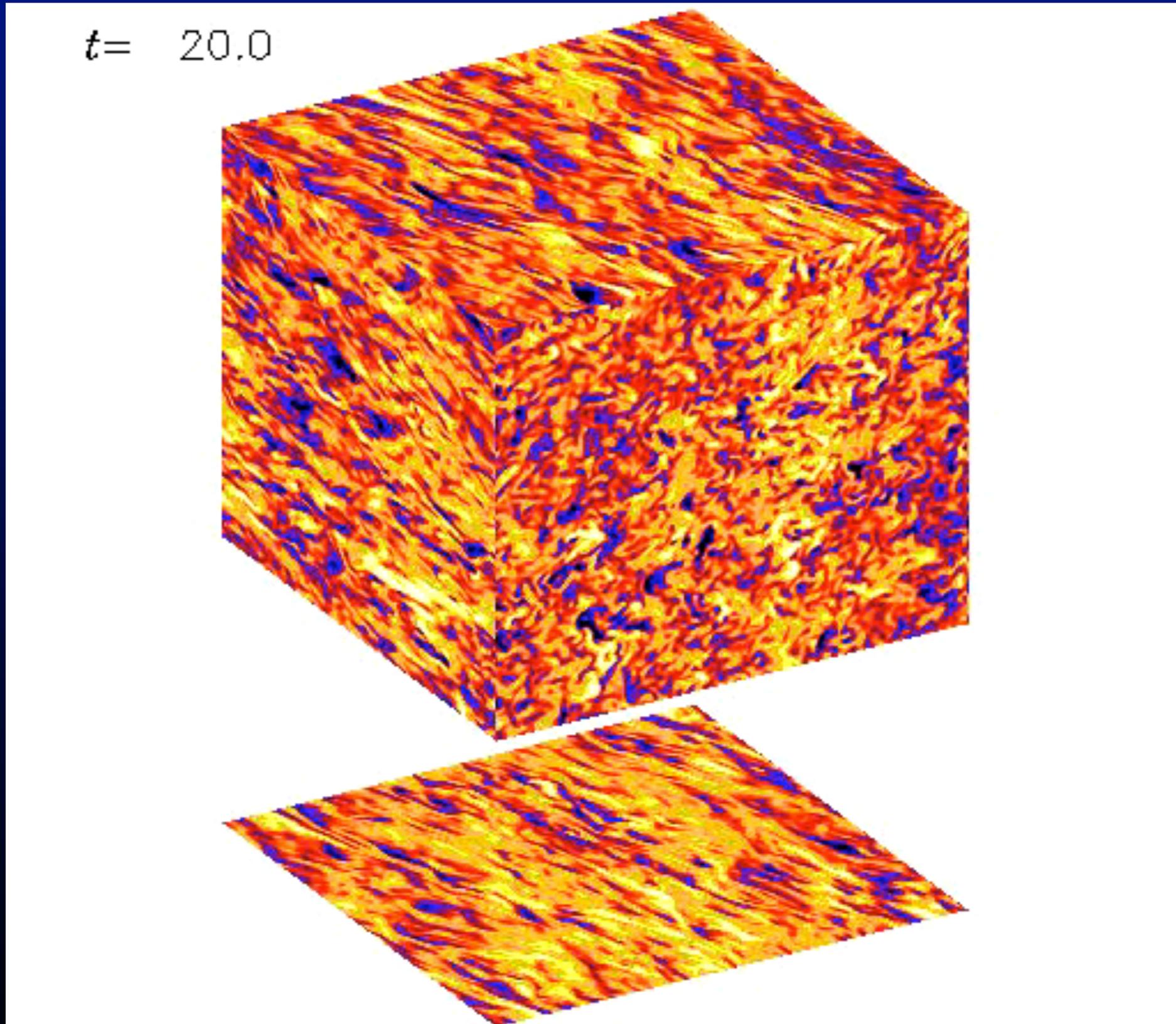


Figure from Balbus (2011)

# Local simulations (ideal MHD)

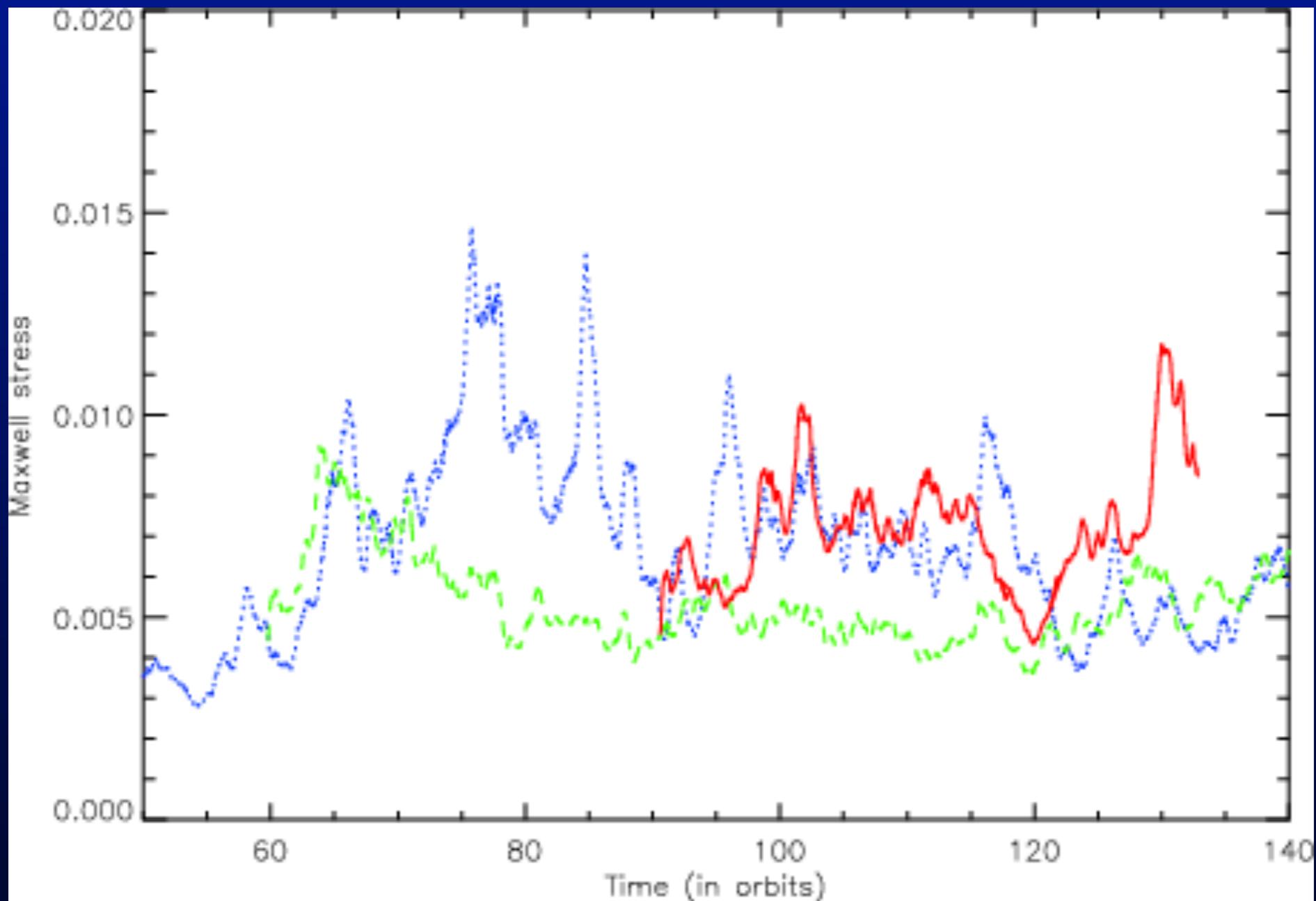


**Animation courtesy of Anders Johansen (Lund)**

# Global simulations (ideal MHD)

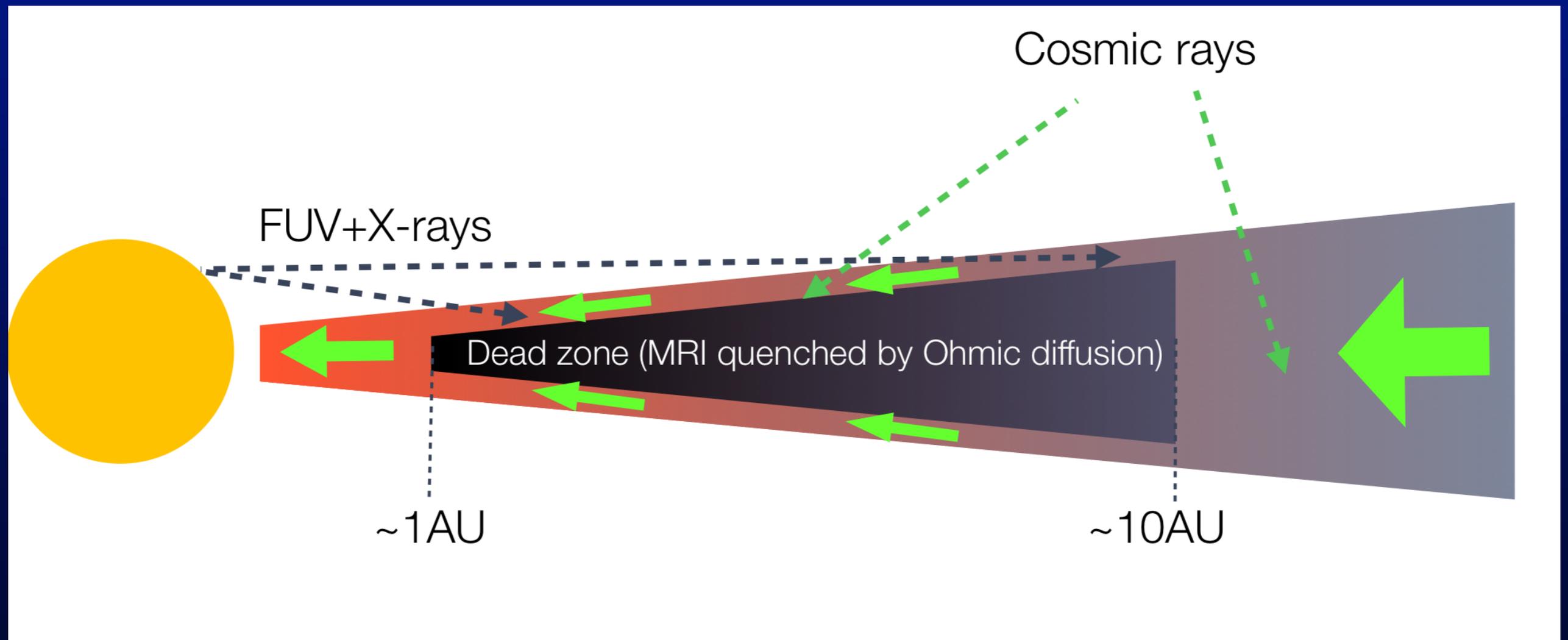
# Accretion and Outflows in 3D Global MHD Simulations of Stratified Protoplanetary Disk

*Mario Flock*  
*Ringberg 2011*



**Figure from Fromang (2010)**

Numerical simulations suggest that (ideal) MRI turbulence can drive angular momentum transport with an “effective alpha” value  $\alpha \sim 0.01$ .



**Figure from Geoffroy Lesur (PP6 talk), after Gammie (1996)**

MRI requires that disc be partially ionized ( $\sim 10^{-12}$ ). The midplane regions of protoplanetary discs may be “MRI dead”, resulting in a layered disc structure.

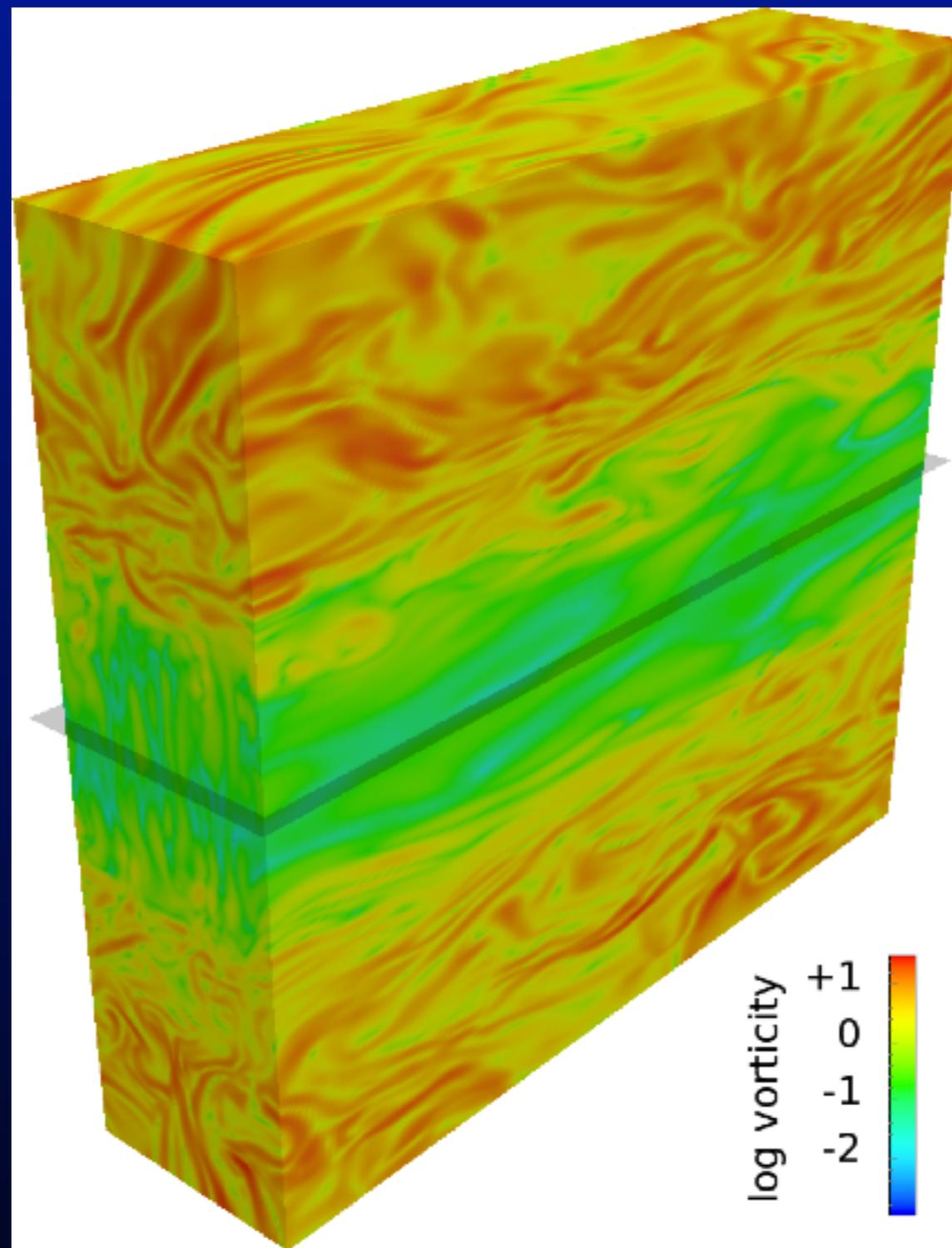
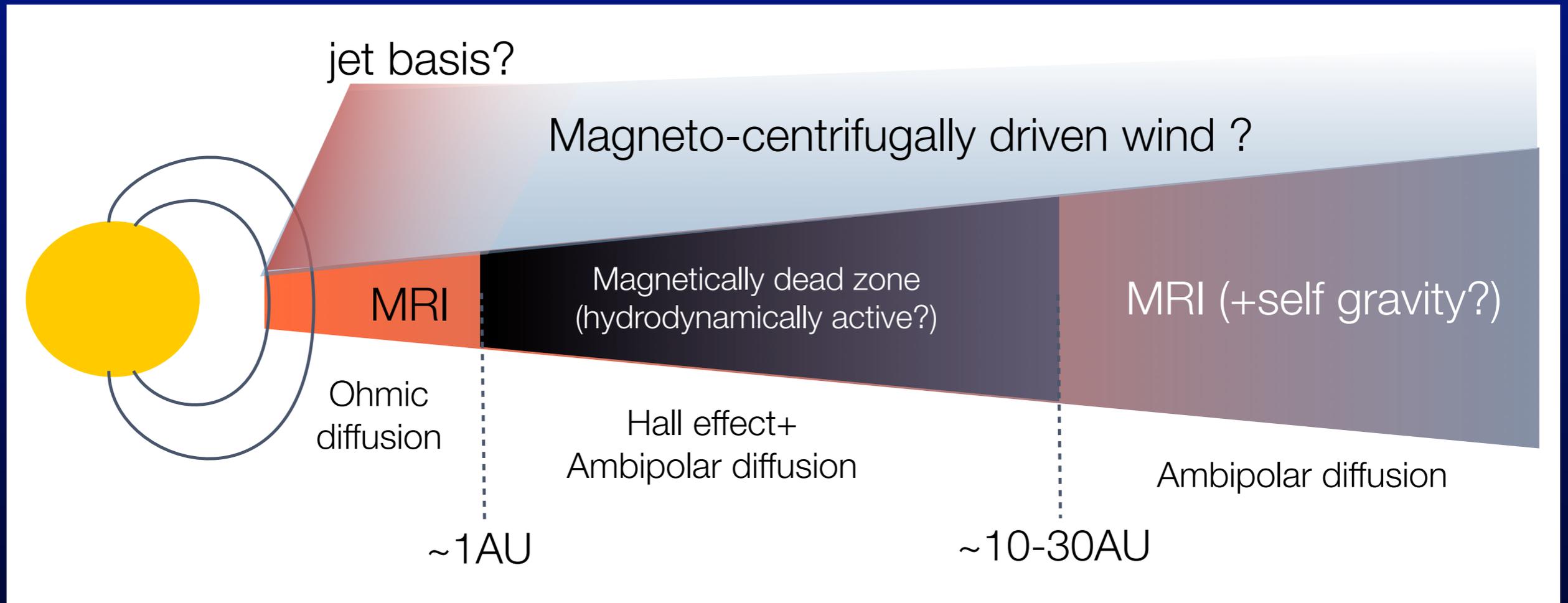


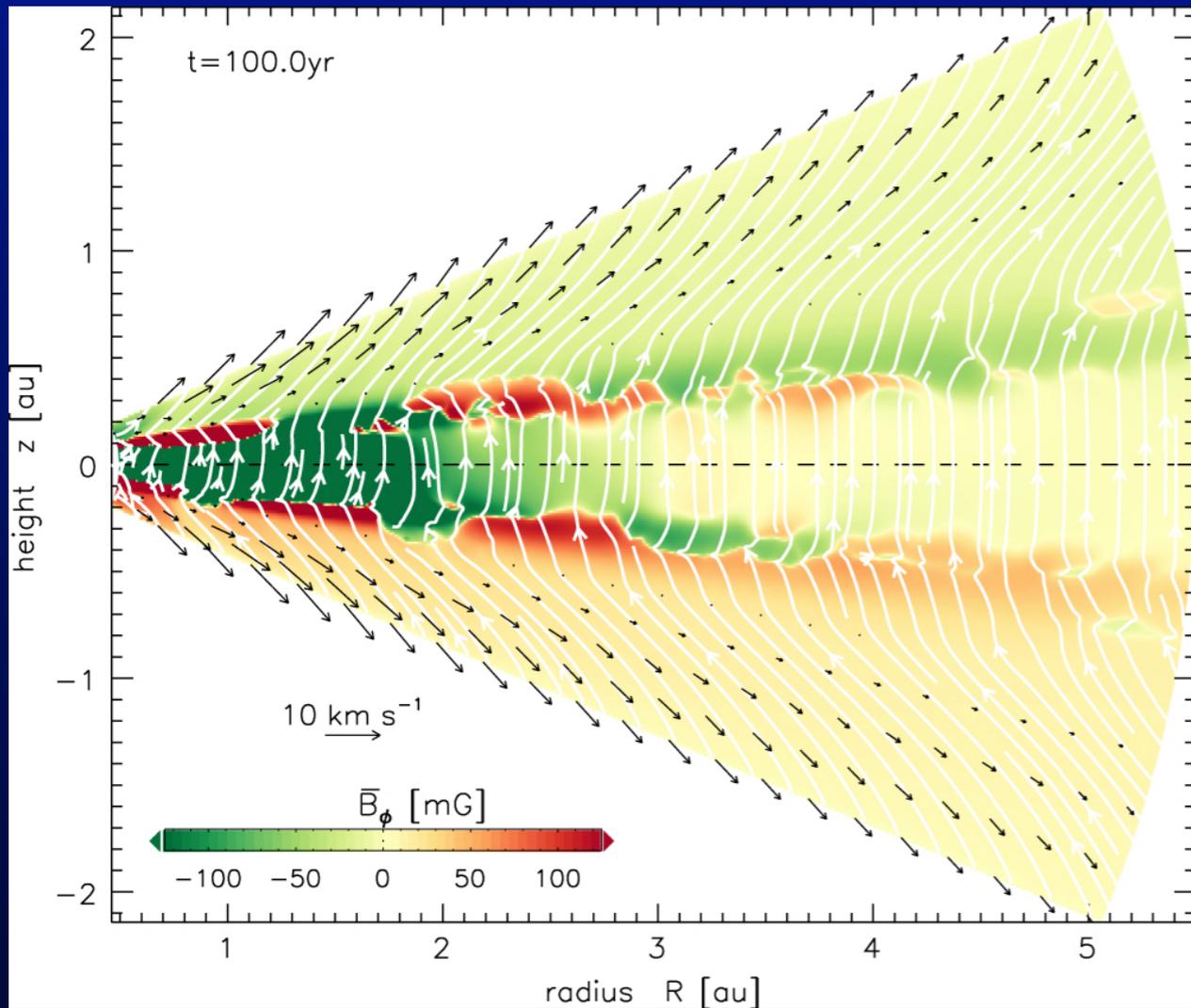
Figure from Gressel, Nelson & Turner (2011)

MRI requires that disc be partially ionized ( $\sim 10^{-12}$ ).  
The midplane regions of protoplanetary discs may be “MRI dead”, resulting in a layered disc structure.

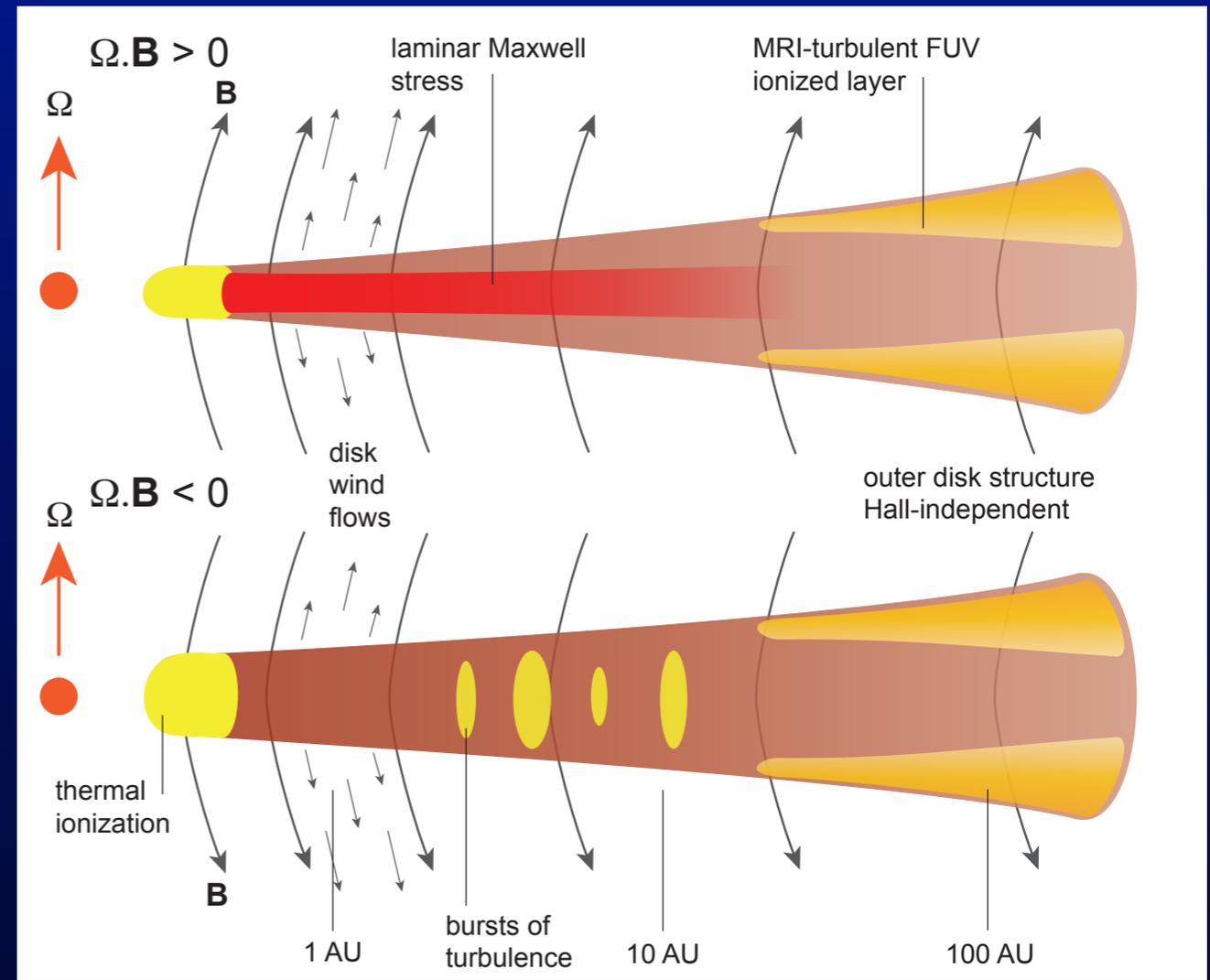


**Figure courtesy of Geoffroy Lesur**

In non-ideal MHD simulations, ambipolar diffusion + a vertical (poloidal) B-field always results in a magnetically-launched disc wind.

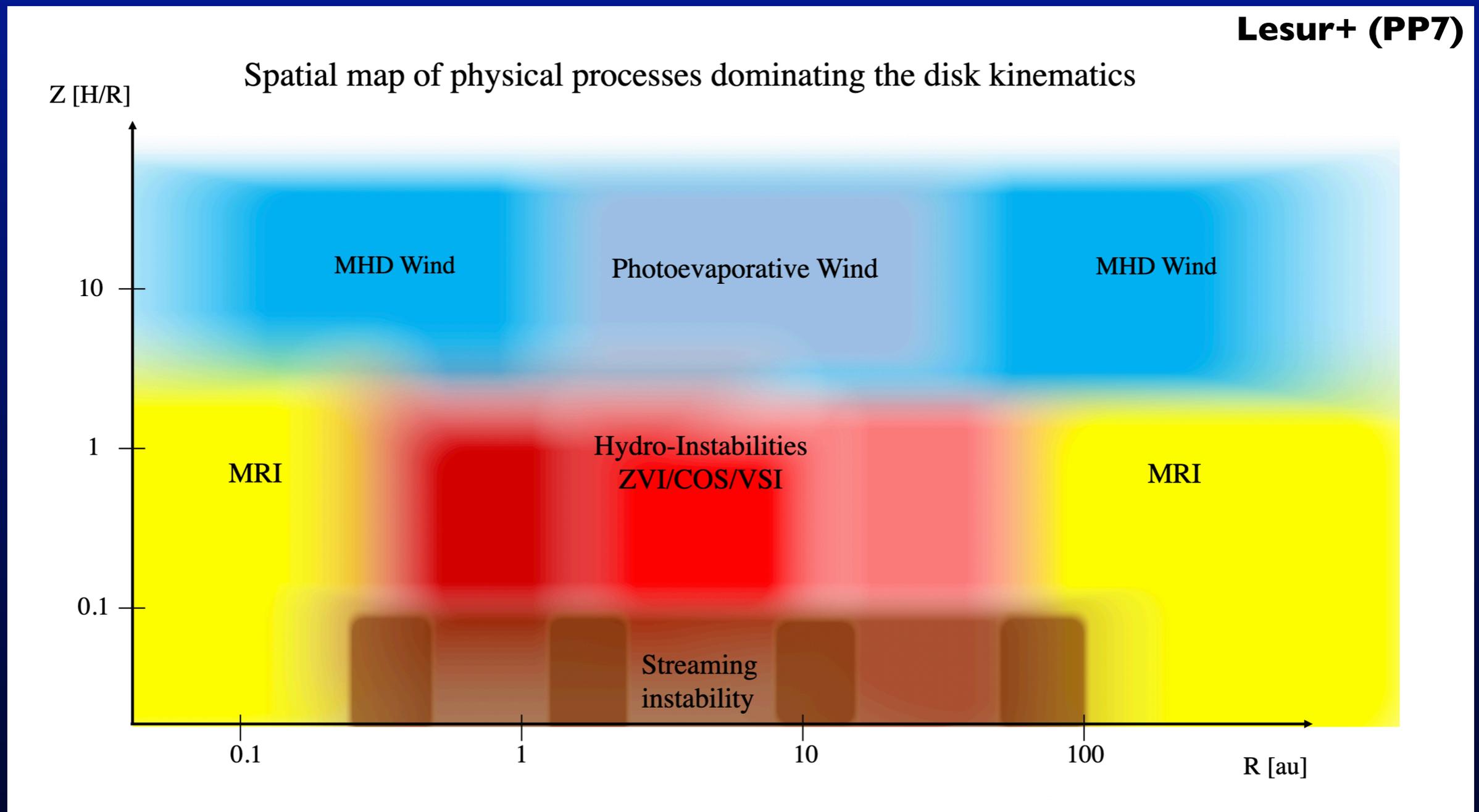


**Gressel+ (2015)**



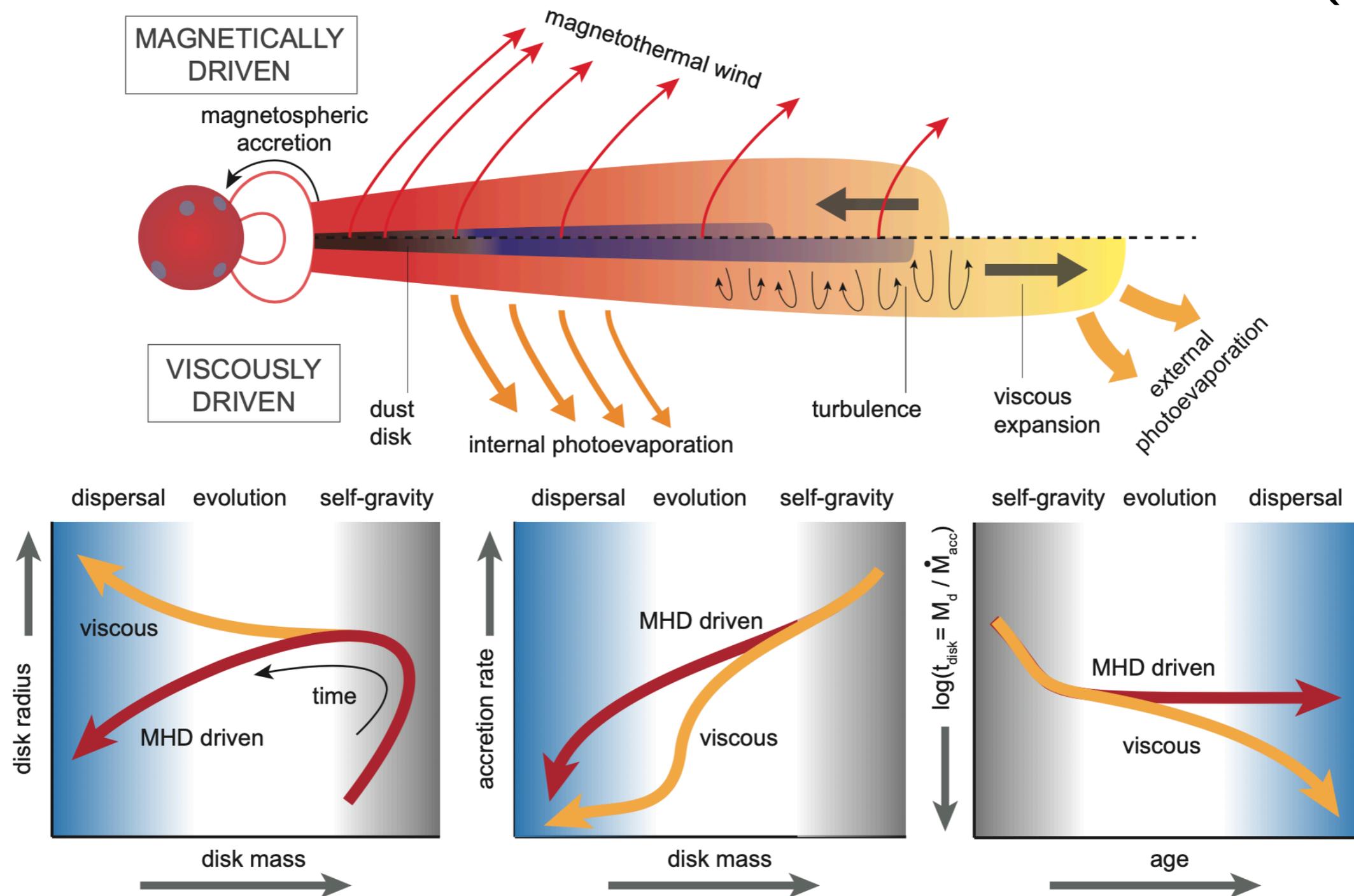
**Simon+ (2015)**

Many uncertainties remain, but broad picture is now largely agreed - “dead zones” always launch winds. Likely that mass-loss is a combination of MRI-wind + photoevaporation: “magneto-thermal wind” (Bai+ 2016).



Dominant transport processes vary with  $R$  and  $z$ , and probably also with time (as disc evolves).

[We'll discuss the streaming instability in Lecture 3.]



It's not clear whether turbulence or the wind torque is the dominant driver of disc accretion/evolution. Most likely both play a role...